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Chapter 10 Geometry: Angles, Triangles, and Distance (3 weeks)

Utah Core Standard(s):

- Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. For example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so. (8.G.5)
- Explain a proof of the Pythagorean Theorem and its converse. (8.G.6) •
- Apply the Pythagorean Theorem to determine unknown side lengths in right triangles in real-world and mathematical problems in two and three dimensions. (8.G.7)
- Apply the Pythagorean Theorem to find the distance between two points in a coordinate system. (8.G.8)

Academic Vocabulary:

right triangle, right angle, congruent, leg, hypotenuse, Pythagorean Theorem, converse of Pythagorean Theorem, simplest radical form, Pythagorean triple, rectangular prism, cube, unit cube, distance formula, vertical angles, adjacent angles, straight angles, supplementary, congruent, parallel lines, *II*, transversal, vertex, point of intersection, corresponding angles, alternate interior angles, alternate exterior angles, similar, angleangle criterion for triangles

Chapter Overview:

This chapter centers around several concepts and ideas related to angles and triangles. In the first section, students will study theorems about the angles in a triangle, the special angles formed when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. They will apply these theorems to solve problems. In Sections 2 and 3, students will study the Pythagorean Theorem and its converse and realize the usefulness of the Pythagorean Theorem in solving many real-world problems. In this chapter, we are referring to these theorems as a collection of facts. The focus in 8th grade is that students are able to observe these facts through examples, exploration, and concrete models. Students will explain why the theorems are true by constructing mathematical arguments, relying on knowledge acquired throughout the year, particularly the properties of rigid motion and dilations and the understanding of congruence and similarity. The explanations and arguments made by students will come in many different forms, including a bulleted list, a narrative paragraph, a diagram without words, and proof by example. They should give their arguments and explanations within their writing and speaking. The emphasis is on students starting to gain an understanding of what makes a good argument or explanation. Can they explain things in a number of different ways? Can they critique the reasoning of others? They should be asking themselves questions such as: What do I know? What is the question asking? Can I draw a model of the situation? Does my argument/explanation have a claim, evidence, and warrant? What is the connection? These practices engaged in by students set the foundation for a more formal study of proof in Secondary II.

Connections to Content:

Prior Knowledge: In elementary grades, students have worked with geometric objects such as points, lines, line segments, rays, angles (right, acute, and obtuse), and perpendicular and parallel lines. They have also studied the different types of triangles (right, acute, and obtuse and equilateral, scalene, and isosceles). They have also learned and used facts about supplementary, complementary, vertical, and adjacent angles. In Chapter 9 of this text, students studied rigid motions and dilations and the definition of congruence and similarity.

Future Knowledge: In Secondary II, students will formally prove many of the theorems studied in this chapter about lines, angles, triangles, and similarity. They will also define trigonometric ratios and solve problems involving right triangles.

MATHEMATICAL PRACTICE STANDARDS (emphasized):

Make sense of problems and persevere in solving them.	What is the relationship between the triangles formed by the dark lines? Justify your answer. Students will use the concrete model shown above in order to make arguments about several of the theorems studied in this chapter. They will also rely on their knowledge of rigid motions and dilations.
Model with mathematics.	A new restaurant is putting in a wheelchair ramp. The landing from which people enter the restaurant is 2 feet higher than street level. Safety standards require that for every 1 foot of rise on a wheelchair ramp there must be a run of 12 feet. How long will the ramp have to be to meet safety standards? Round your answer to the nearest tenth. <i>Students will apply the Pythagorean Theorem in order to solve many real-</i> <i>world problems. They will have to analyze the situation to determine if the</i> <i>Pythagorean Theorem can be used to solve the problem, draw a picture of the</i> <i>situation, analyze givens and constraints, and understand what they are</i> <i>solving for.</i>
Construct viable arguments and critique the reasoning of others.	Suppose you are given two lines <i>j</i> and <i>k</i> in the picture below. You have been asked to determine whether the two lines are parallel. You start by drawing the transversal <i>l</i> through the two lines as shown below. Devise a strategy to determine whether the two lines are parallel using what you know about the properties of rigid motion. Next, use your strategy to determine whether lines <i>d</i> and <i>e</i> are parallel. Just saying they do not look parallel, is not a justification.

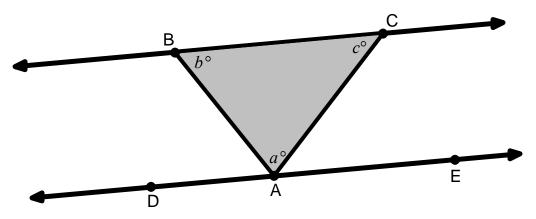
	Attend to Precision	Find, Fix, and Justify: Megan was asked to solve for the unknown side length in the triangle below. Her work is shown below. She made a mistake when solving. Explain the mistake she made and then solve the problem correctly. $\frac{Megan's Solution:}{a^2 + b^2 = c^2}$ $5^2 + 13^2 = c^2$ $25 + 169 = c^2$ $194 = c^2$ $\sqrt{194} = c$ This problem requires that students are clear in their understanding of the Deducement Theorem and here to use it to solve for the unknown side
	Use appropriate tools strategically.	Pythagorean Theorem and how to use it to solve for missing side lengths. Use ideas of rigid motion to prove that $\angle 1 \cong \angle 3$ and $\angle 2 \cong \angle 4$. Students will rely heavily on the knowledge learned in Chapter 9 about rigid motions and congruence and dilations and similarity. This knowledge will be a tool they apply to understand and informally prove many of the theorems about angles, triangles, and similarity in this chapter.
n#	Reason abstractly and quantitatively.	<i>about angles, triangles, and similarity in this chapter.</i> a = b = b = a = b = b = a = a

		Use the picture below to answer questions a) and b).
┍╴╴	Look for and express regularity in repeated reasoning.	 a. Find all the missing side lengths and label the picture with the answers. b. Using the picture above, devise a strategy for constructing a segment with a length of √5. Explain your strategy below. In this problem, students should start to notice that the hypotenuse of the new triangle will follow a pattern. This observation gives them a process for constructing any segment of length √n where n is a whole number.
		Given that line $w \parallel$ line v , determine if the triangles given below are similar. If they are similar justify why.
	Look for and make use of structure.	In the problem above students must look at the geometric figure above and evaluate the information given to them. They are given that line w line v. They must recognize that the two intersecting lines that form the triangles are transversals of the parallel lines. Students might do this by extending the transversals beyond the interior of the two parallel lines or by drawing an auxiliary line over these lines that extends beyond the parallel lines. Once they look at these lines as transversals they can use what they know about special angle relationships to determine congruence amongst angles within the triangles. As students view the structure of the intersecting lines their perspective shifts and they are able to derive more information about the figure.

10.0 Anchor Problem: Reasoning with Angles of a Triangle and Rectangles

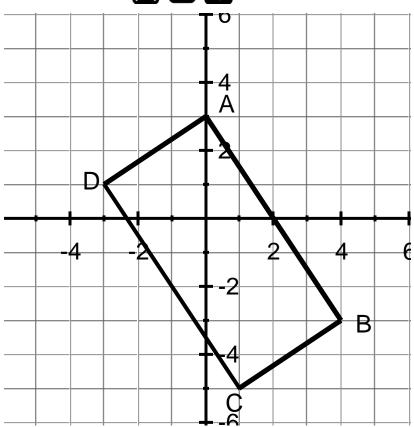
Part I

Given that $\overrightarrow{BC} \parallel \overrightarrow{DE}$ in the picture below, show that $a + b + c = 180^{\circ}$.



Part II

Pedro's teacher asks him to classify the quadrilateral below. He claims it is a rectangle. His teacher tells him to give a good argument and explanation. Help Pedro to support his claim using mathematical evidence. **Remember:** Opposite sides of a rectangle have the same length and are parallel and the sides of a rectangle meet at right angles.



10.1 Angles and Triangles

Section Overview:

The focus of this section is on the development of geometric intuition through exploration with rigid motions and dilations. Through exploration, observation, and the use of concrete models, students will analyze facts about triangles and angles and use these facts to describe relationships in geometric figures. There will also be a focus on making sound mathematical explanations and arguments in order to verify theorems about angles and triangles and when explaining and justifying solutions to problems throughout the section.

Concepts and Skills to Master:

By the end of this section, students should be able to:

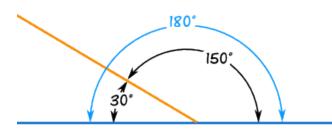
- 1. Know that straight angles sum to 180° and that vertical angles are congruent.
- 2. Know that the sum of the angles in a triangle is 180°. Understand that the measure of an exterior angle of a triangle is equal to the sum of the measures of the non-adjacent angles. Use these properties to find missing angle measures related to a triangle.
- 3. Determine the relationship between angles formed when a transversal intersects parallel lines. Use these relationships to find missing angle measures.
- 4. Determine whether two lines are parallel based on the angle measures when a transversal intersects the lines.
- 5. Understand and apply the angle-angle criterion to determine whether two triangles are similar.

10.1a Class Activity: Straight and Vertical Angles Review

In this section, you will observe and use several different geometric facts learned in previous grades. They will be denoted using bullets.

• Angles that lie on the same line (straight angles) are supplementary.

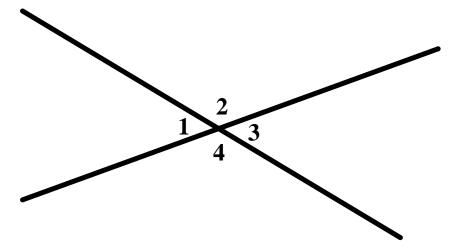
In 7th grade, you learned that a straight angle has a measure of 180° as shown below. Angles that sum to 180° are **supplementary**. In the picture below, 30° and 150° are supplementary and together they form a straight angle.



• Vertical angles have the same measure.

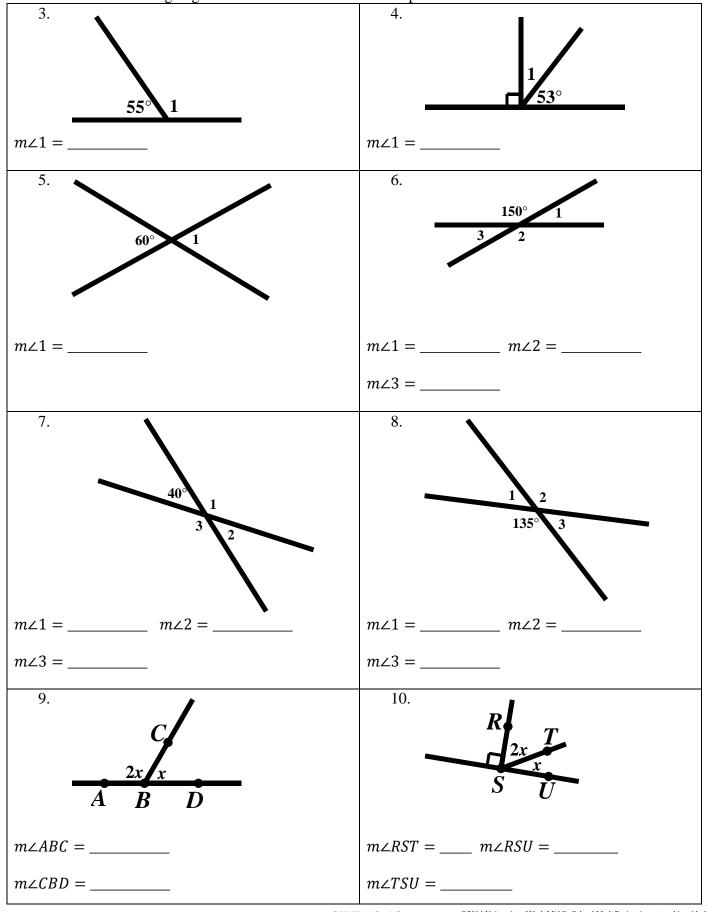
Vertical angles are the opposing angles formed by two intersecting lines.

In the picture below, $\angle 1$ and $\angle 3$ are vertical angles and $\angle 2$ and $\angle 4$ are vertical angles.



1. Show that $\angle 1 \cong \angle 3$ and $\angle 2 \cong \angle 4$. (Hint: Think about ideas of rigid motion and straight angles.)

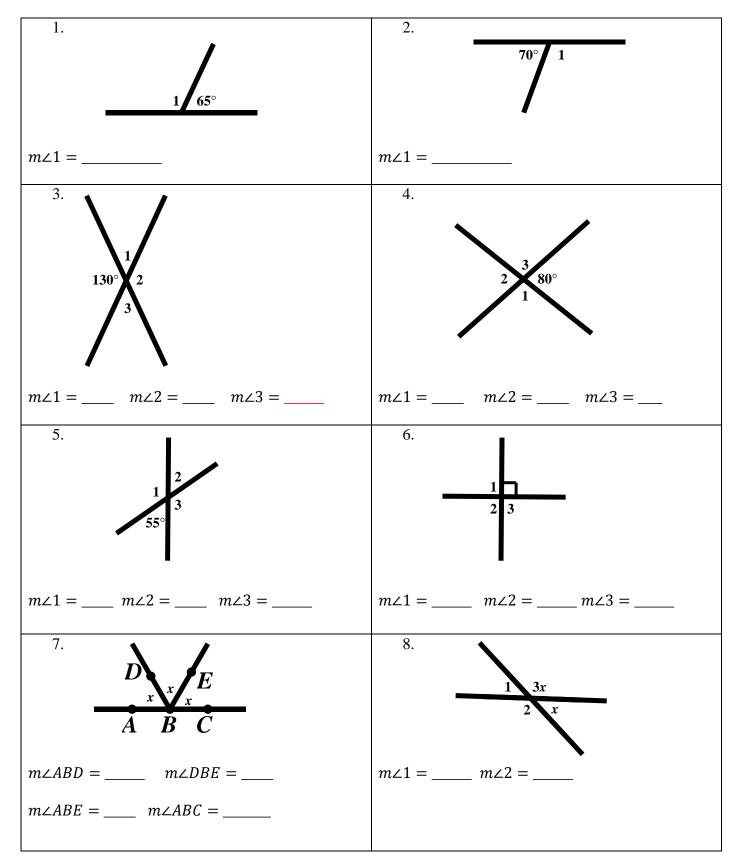
Review: Find the missing angle measures without the use of a protractor.



8WB10-10

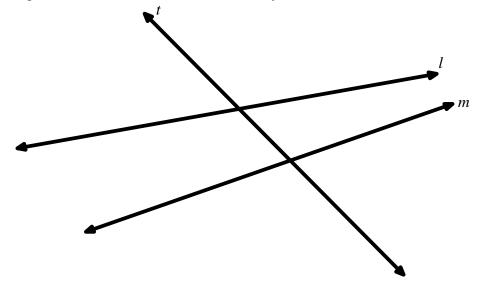
10.1a Homework: Straight and Vertical Angles Review

Review: Find the missing angle measures without the use of a protractor.



10.1b Class Activity: Special Angles Formed by Transversals

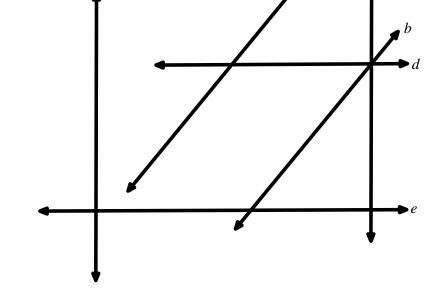
1. In the picture given below line *l* and line *m* are cut by a transversal line called *t*.



- 2. Define transversal in your own words. Draw another transversal for the two lines above and label it line *r*..
- 3. Some of the runways at a major airport are shown in the drawing below. Identify at least 2 sets of lines to which each line is a transversal.

8WB10-12

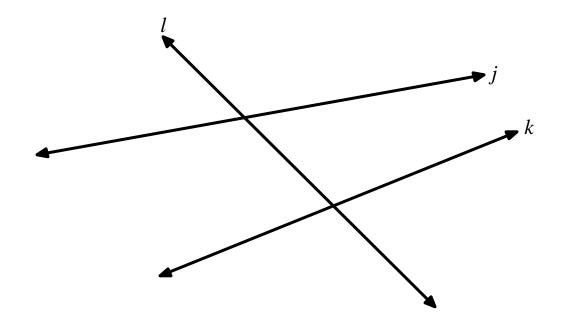
- *a*. line *a*
- b. line *b*
- c. line *c*



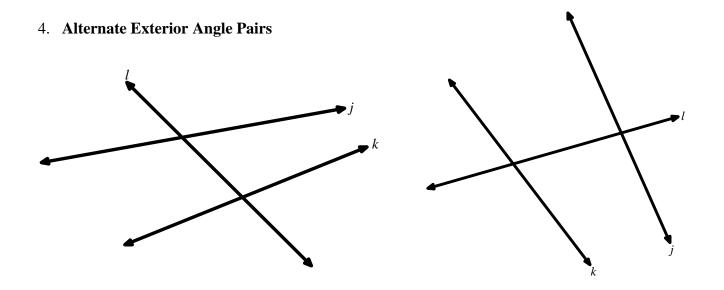
d. line *e*

a

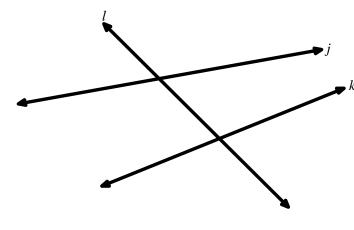
When two lines are intersected by a transversal there are special angle pairs that are formed. Use the angle names provided by your teacher to move the angle names around the picture below until you think you have found its correct location. Be ready to justify your reasoning. There will be several correct locations for each set of angle pairs and more than one term may fit at an angle.

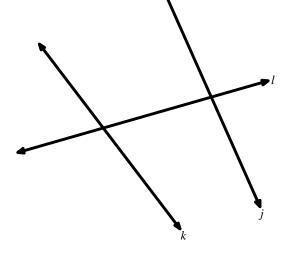


Directions: Color code the following sets of angles by coloring each set of angle pairs the same color. Find at least two sets of the special angles for each drawing.

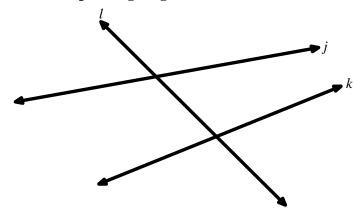


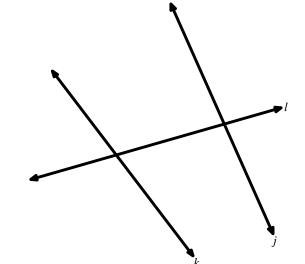
5. Alternate Interior Angle Pairs



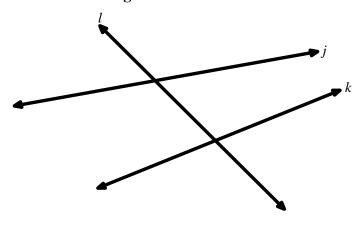


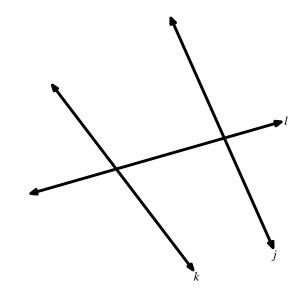
6. Corresponding Angle Pairs



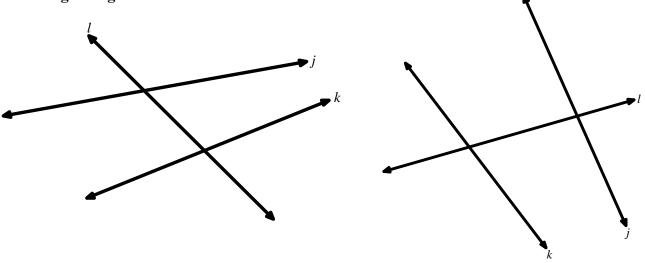


7. Vertical Angle Pairs

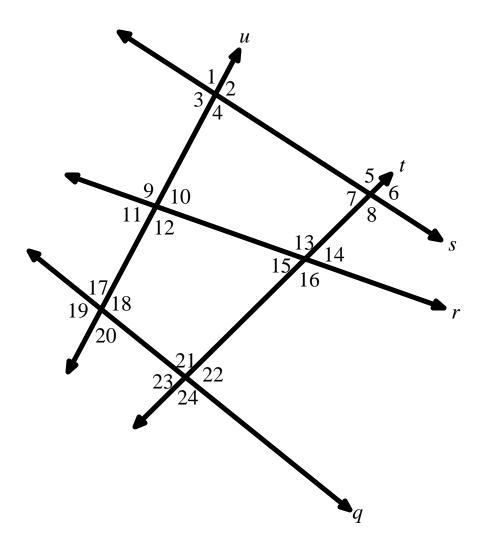




8. Straight Angle Pairs

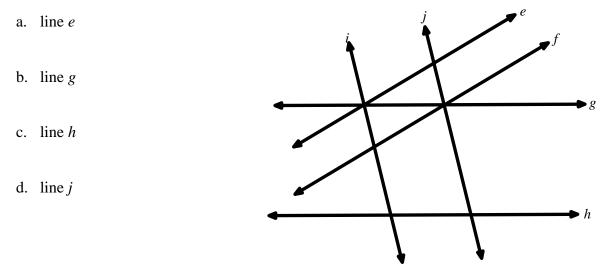


- 9. Refer to the figure below; identify the following pairs of angles as alternate exterior angles, alternate interior angles, corresponding angles, vertical angles, or straight angles.
 - a. $\angle 1$ and $\angle 8$
 - b. $\angle 12$ and $\angle 11$
 - c. $\angle 13$ and $\angle 21$
 - d. $\angle 14$ and $\angle 15$
 - e. $\angle 7$ and $\angle 14$
 - f. $\angle 9$ and $\angle 20$
 - g. $\angle 5$ and $\angle 7$
 - h. $\angle 22$ and $\angle 23$
 - i. $\angle 1$ and $\angle 5$
 - j. $\angle 21$ and $\angle 8$

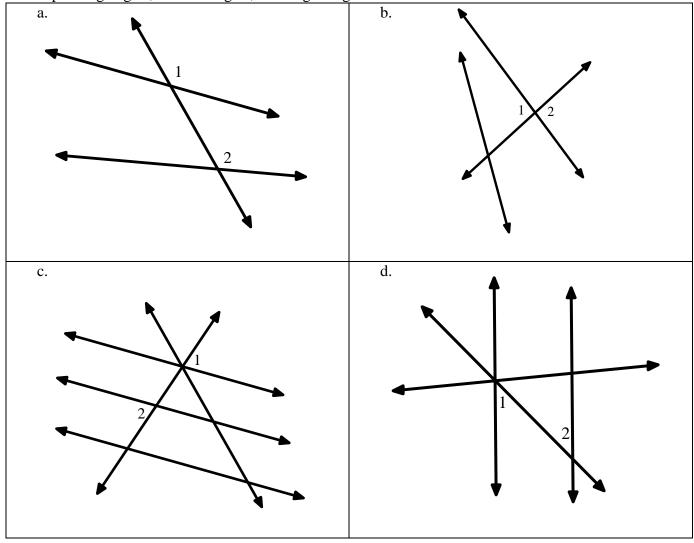


10.1b Homework: Special Angles Formed by Transversals

1. Identify the sets of given lines to which each line is a transversal.



2. Refer to the figures below. State if $\angle 1$ and $\angle 2$ are alternate exterior angles, alternate interior angles, corresponding angles, vertical angles, or straight angles.



3. Refer to the figure below; state if the following pairs of angles are alternate exterior angles, alternate interior angles, corresponding angles, vertical angles, or straight angles.

3

4

6

7

9

11

10

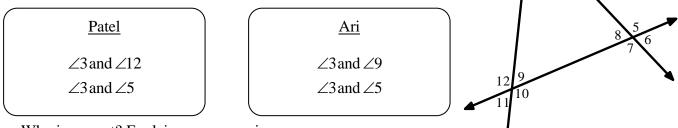
12

т

- a. $\angle 4$ and $\angle 9$
- b. $\angle 12$ and $\angle 11$
- c. $\angle 1$ and $\angle 5$
- d. $\angle 1$ and $\angle 8$
- e. $\angle 6$ and $\angle 7$
- f. $\angle 1$ and $\angle 3$
- g. $\angle 8$ and $\angle 9$
- h. $\angle 7$ and $\angle 11$
- i. $\angle 3$ and $\angle 10$
- j. $\angle 10$ and $\angle 11$

Find, Fix, and Justify

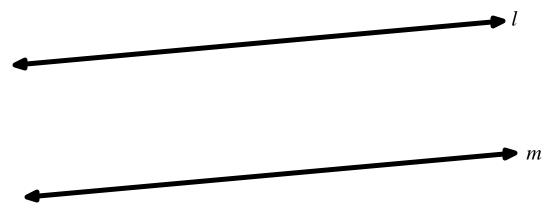
4. Patel and Ari are naming alternate interior angles for the figure below. They are listing alternate interior angle pairs for angle 3. Their work is shown below.



Who is correct? Explain your reasoning.

10.1c Class Activity: Parallel Lines and Transversals

1. Use the picture given below to describe what parallel lines are. Use the correct notation to denote that line l is parallel to line m.



2. Draw a transversal for the two parallel lines above and label it line *t*. Label the angles formed by the transversal and the parallel lines with numbers 1 through 6. *Be sure to number in the same order as your teacher.

Transversals that intersect two or more parallel lines create angle pairs that have special properties. Use what you know about rigid motions to discover some of these relationships.

3. What type of angle pair is $\angle 2$ and $\angle 6$?

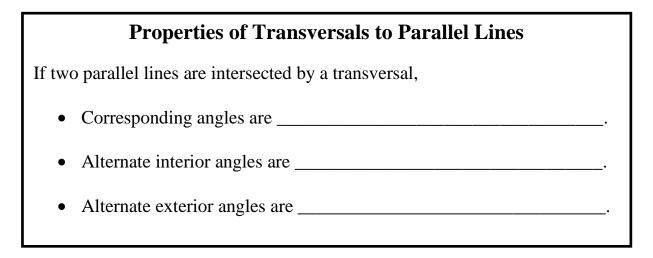


- 4. Copy ∠2 on a piece of tracing paper (or patty paper). Describe the rigid motion that will carry ∠2 to ∠6. Determine the relationship between ∠2 and ∠6.
- 5. Use a similar process to see if the same outcome holds true for all of the corresponding angles in the figure. Start by listing the remaining pairs of corresponding angles and then state the relationship.

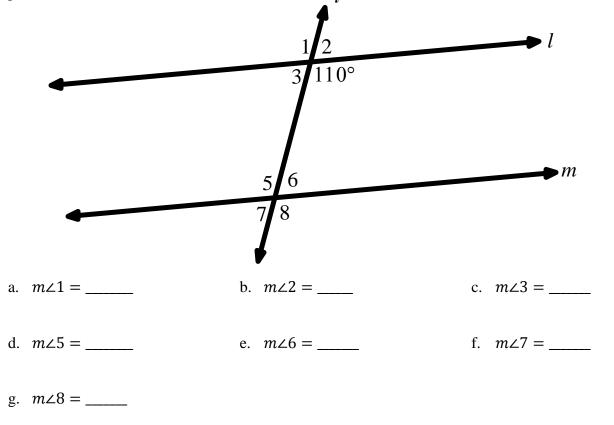
6. List the pairs of angles that are vertical angles, what do you know about vertical angles?

7. Continue to use rigid motions and what you know about vertical angles to discover other relationships that exist between alternate interior angles and alternate exterior angles. Be sure to provide justification for your claims.

8. Complete the following statements in the box below.

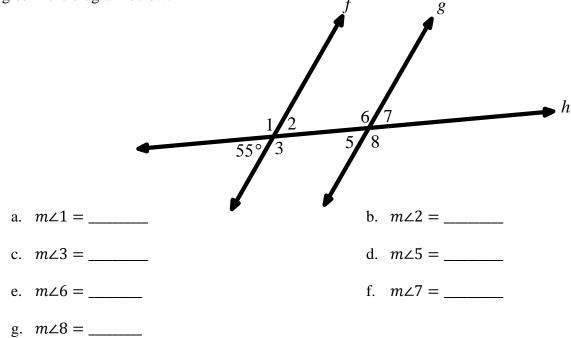


9. In the diagram below one angle measure is given. Find the measure of each remaining angle if line *l* is parallel to line *m*.

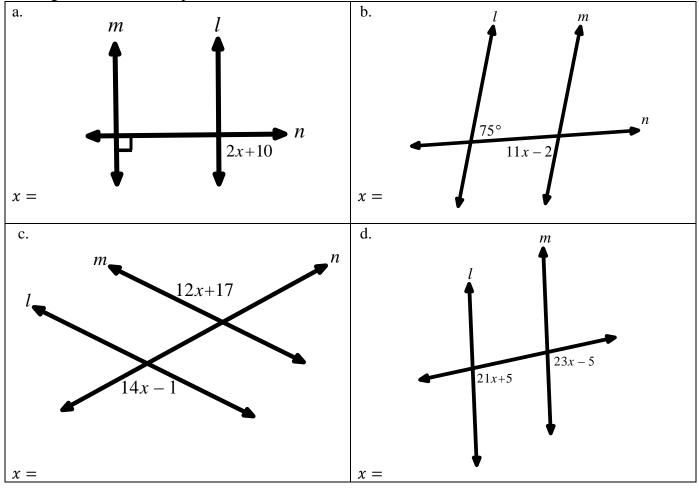


8WB10-19

10. Line $f \parallel$ line g and one angle measure is given in the diagram. Determine the measures of the remaining angles in the diagram below.



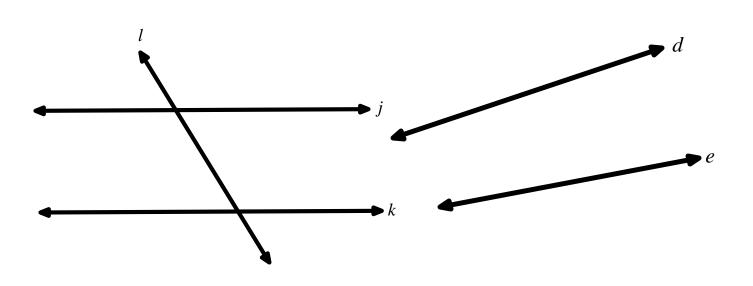
11. Given that line $l \parallel$ line *m* solve for *x* and then find the measure of all the remaining angles. Write the angle measures on the picture.



8WB10-20

12. Given two lines j and k in a picture below with transversal l devise a strategy to determine whether the two lines are parallel using what you know about the properties of rigid motion. Also use your strategy to determine whether lines d and e are parallel. Stating that the lines do not look parallel, is not a justification.

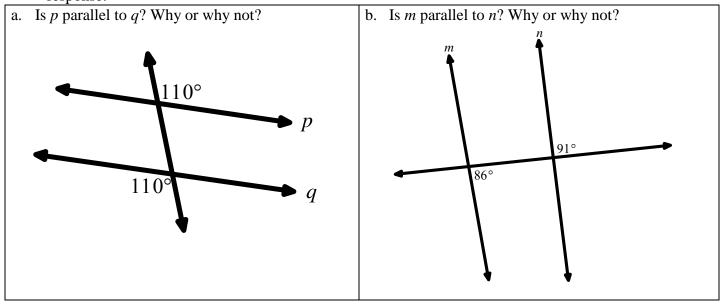




13. Complete the statement below.

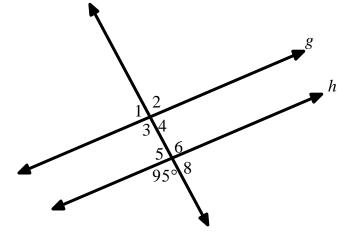
Given two lines, if a transversal cuts through both lines so that corresponding angles are_____, then the two lines are ______

14. Determine whether the following sets of lines are parallel or not. Provide a justification for your response.



10.1c Homework: Parallel Lines and Transversals

Directions: Use the diagram below to answer questions #1 and 2 given that $g \parallel h$.

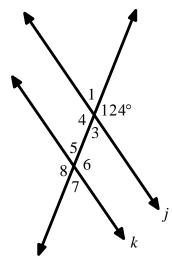


- 1. For each of the following pairs of angles, describe the relationship between the two angles (corresponding angles, alternate interior angles, alternate exterior angles, or vertical angles).
 - a. $\angle 3 \text{ and } \angle 6$ b. $\angle 4 \text{ and } \angle 8$
 - c. $\angle 1$ and $\angle 8$ d. $\angle 1$ and $\angle 5$
- 2. One angle measure is given in the diagram. Determine the measures of the remaining angles in the diagram.
 - a. $m \angle 1 = _$ b. $m \angle 2 = _$

 c. $m \angle 3 = _$ d. $m \angle 4 = _$

 e. $m \angle 5 = _$ f. $m \angle 6 = _$
 - g. *m*∠8 = _____

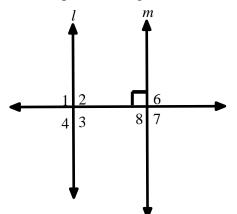
Directions: Use the diagram below to answer question #3 given that line $j \parallel$ line k.



3. One angle measure is given in the diagram. Determine the measures of the remaining angles in the diagram.

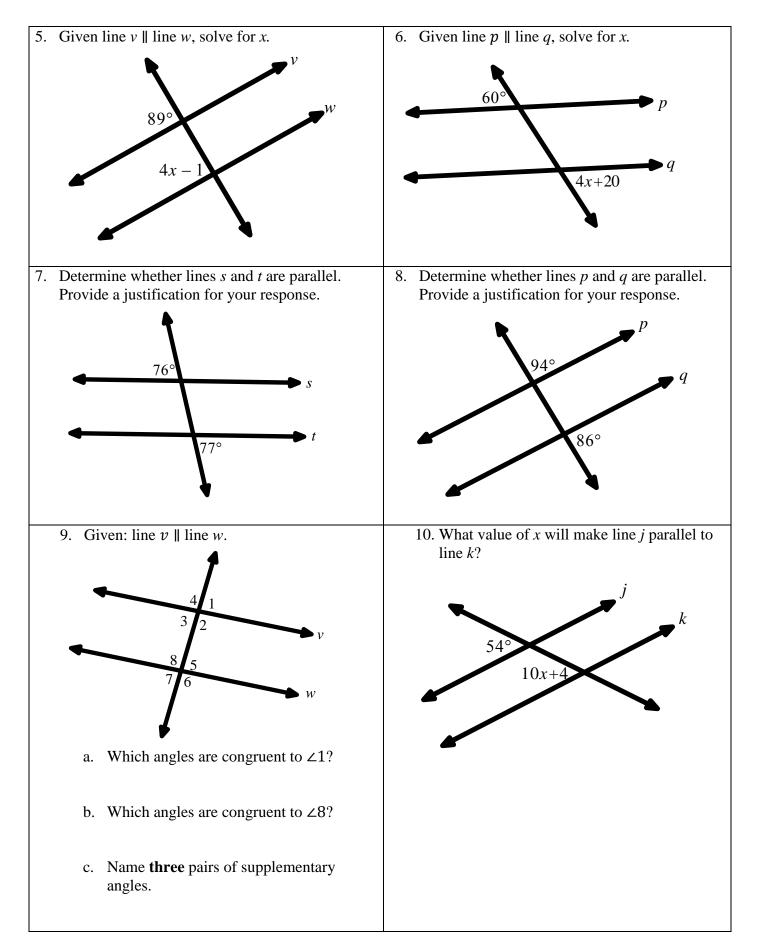


Directions: Use the diagram below to answer question #4 given that line $l \parallel$ line m.



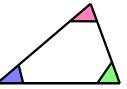
- 4. One angle measure is given in the diagram. Determine the measures of the remaining angles in the diagram.
 - b. *m*∠2 = _____ a. $m \angle 1 =$
 - c. *m*∠3 = _____ d. *m*∠4 = _____
 - e. *m*∠6 = _____
 - g. *m*∠7 = _____

- f. *m*∠8 =



10.1d Class Activity: Tesselating Triangles

- 1. Take the index card that has been given to you and using a ruler draw an obtuse scalene triangle or an acute scalene triangle. Remember, in a scalene triangle, the side lengths of the triangle are all different. If the triangle has to be acute or obtuse, that means it can't have a right angle.
- 2. Cut out the triangle and color the angles each a different color as shown below.



3. Tessellate an 8 ¹/₂" x 11" white piece of paper with copies of your triangle. A **tessellation** is when you cover a surface with one or more geometric shapes, called tiles, with no overlaps or gaps. A tessellation by regular hexagons is shown below.



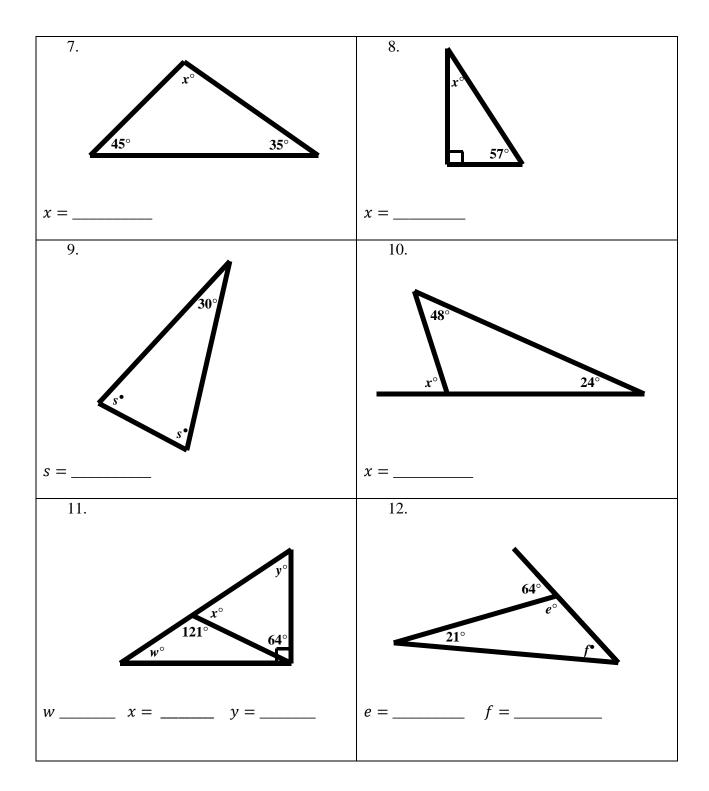
After each tessellation of your triangle, color each angle with its corresponding color.

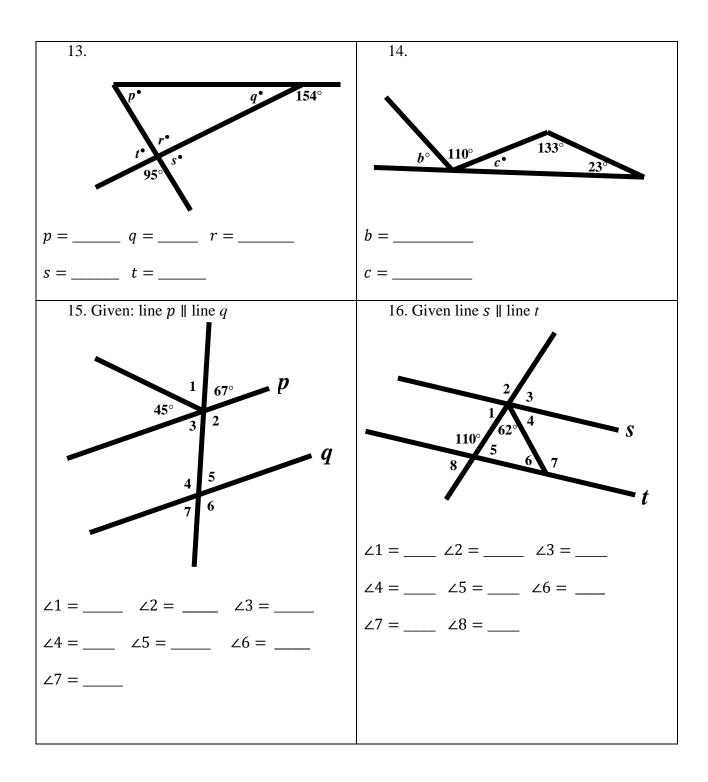
4. What types of motion did you use to tessellate the plane with your triangle?

- 5. Look back at some of the facts we have studied so far in this section. How does your tessellation support these facts?
- Angles that lie on the same line are supplementary and have a common vertex. •
- Vertical angles have the same measure.
- If two lines are parallel and they are intersected by a transversal, then corresponding angles at the • points of intersection have the same measure.
- Given two lines, if a third line cuts through both lines so that corresponding angles are congruent, • then the two lines are parallel.

- 6. The following bolded bullets are additional facts we can observe in our tessellation. Use your tessellation to obverse each fact and then provide a mathematical explanation as to why each fact is true.
- The sum of the interior angles of a triangle is a straight angle (180°).
- The sum of the interior angles of a quadrilateral is 360°.
- The measure of an exterior angle of a triangle is equal to the sum of the measures of the non-٠ adjacent angles.

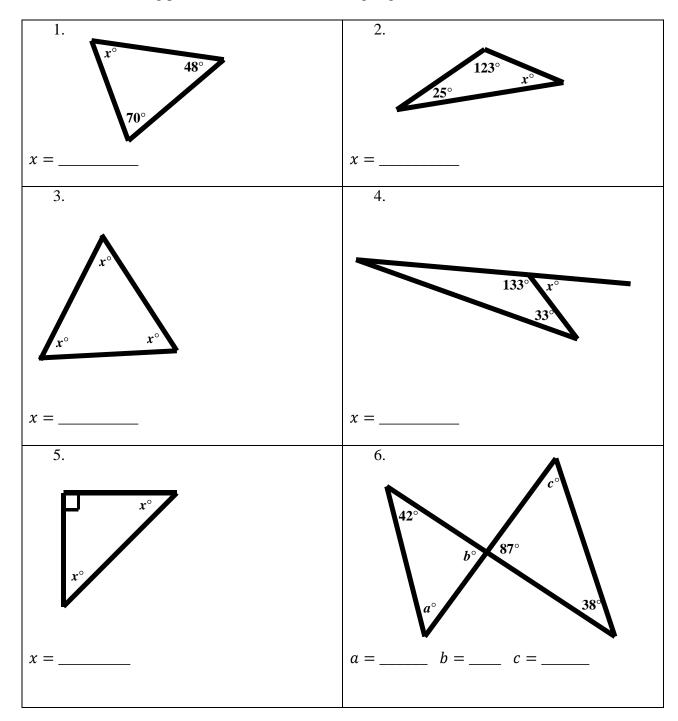
Directions: In the following problems, solve for the missing angle(s).

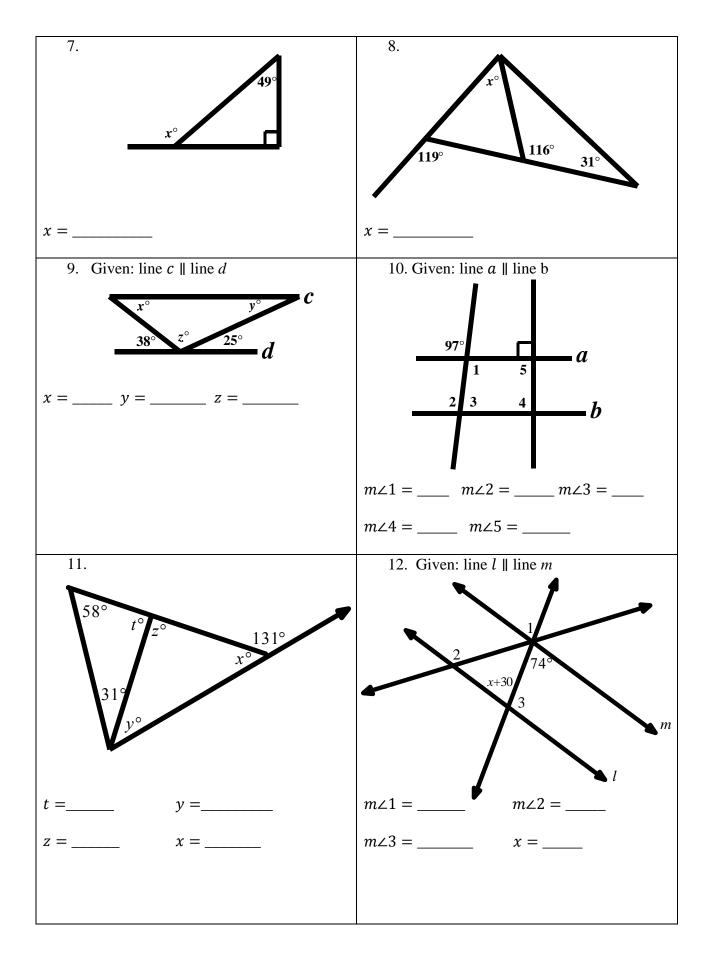




10.1d Homework: Finding Angle Measures in Triangles

Directions: In the following problems, solve for the missing angle(s).



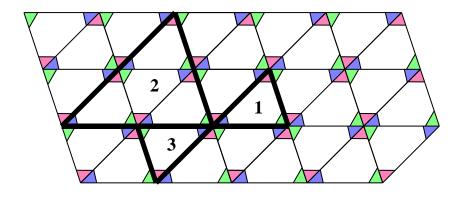


10.1e Class Activity: Similar Triangles

Revisit some of the following facts about similar triangles from Chapter 9.

- If two triangles are similar, then the ratios of the lengths of corresponding sides are the same.
- If two triangles are similar, then corresponding angles have the same measure.

Use the tessellation you made to continue your study of triangles.



- 1. In Chapter 9 we learned that if one figure can be carried onto another by a series of rigid motions and dilations, then the two figures are similar.
 - a. In the picture above triangle 1 is similar to triangle 2. Describe the sequence of transformations that will carry triangle 1 onto triangle 2. What is the scale factor?
 - b. In the picture above triangle 2 is similar to triangle 3. Describe the sequence of transformations that will carry triangle 2 onto triangle 3. What is the scale factor?
 - c. What do you notice about the corresponding angles of similar triangles?
- 2. Can you find a triangle that is a dilation of triangle 1 with a scale factor of 3? Trace the triangle. What do you notice about the angle measures in the new triangle you created?

Below is another fact about similar triangles.

- Given two triangles, if the corresponding angles have the same measure, then the triangles are similar.
- 3. We will be using the tessellation you made to explore the proposition above. Find and highlight in black two triangles that have the same angle measures but are a different size.

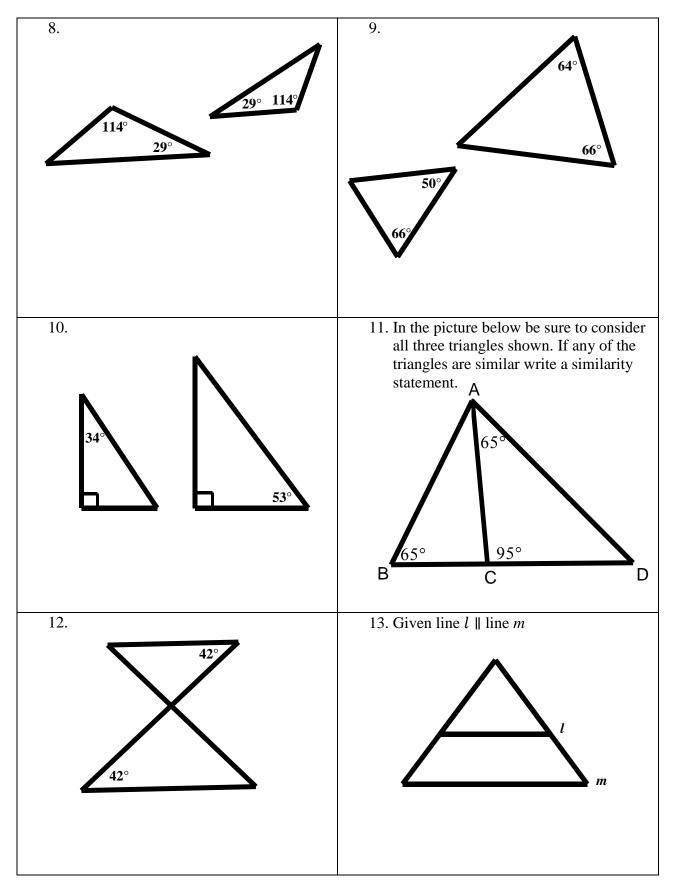
- 4. What is the relationship between the triangles formed by the dark lines? Justify your answer.
- 5. Find a third triangle that is a different size than the other two you highlighted. Highlight the third triangle. What is the relationship of this triangle to the other triangles? Justify your answer.
- 6. Complete the following statement. It two triangles have corresponding angles that are the same measure,

then one triangle can be mapped to the other using _____; therefore the triangles

are _____.

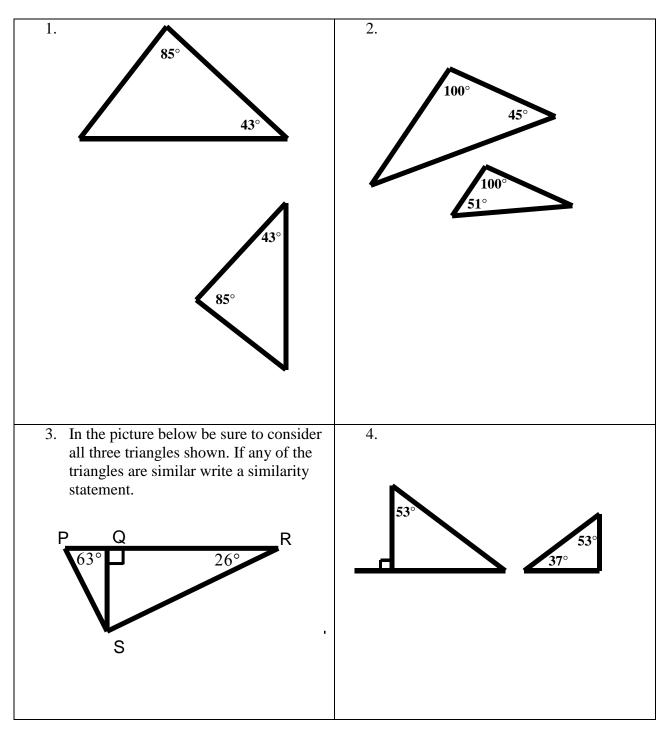
7. Do all 3 pairs of corresponding angles have to be congruent in order to say that the two triangles are similar? What if only 2 pairs of corresponding angles are congruent? Would the triangles still be similar? Why or why not?

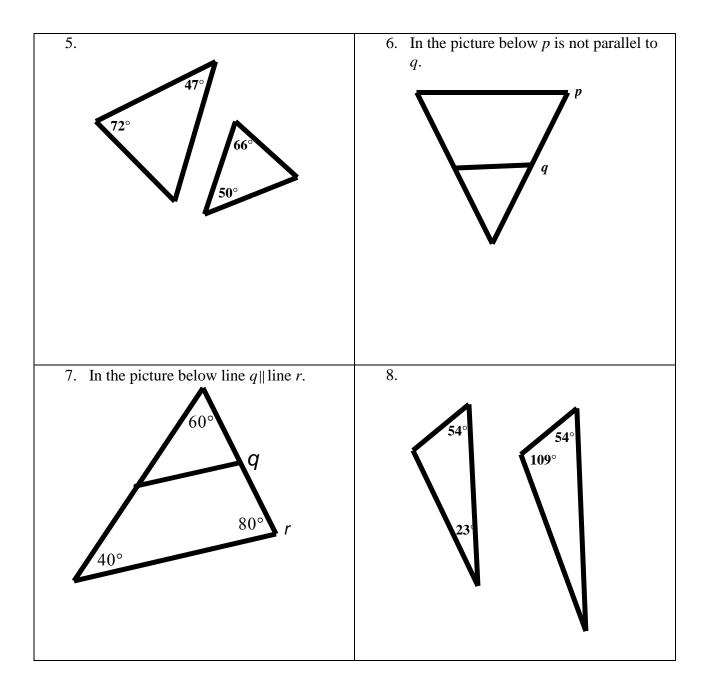
Directions: Are the triangles similar? If they are similar justify why.



10.1e Homework: Similar Triangles

Directions: Are the triangles similar? If they are similar justify why.





10.1f Self-Assessment: Section 10.1

Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept. Sample problems are provide on the next page.

Section of the secti				
Skin/Concept	Understanding	Understanding	Understanding	Understanding
	1	2	3	4
1. Know that straight	-	-		•
angles sum to 180°				
and that vertical				
angles are congruent.				
See sample problem #1				
2. Know that the sum of				
the angles in a				
triangle is 180°.				
Understand that the				
measure of an				
exterior angle of a				
triangle is equal to				
the sum of the				
measures of the non-				
adjacent angles. Use				
these properties to				
find missing angle				
measures related to a				
triangle.				
See sample problem #2				
3. Determine the				
relationship between				
angles formed when a				
transversal intersects				
parallel lines. Use				
these relationships to				
find missing angle				
measures.				
See sample problem #3				
4. Determine whether				
two lines are parallel				
based on the angle				
measures when a				
transversal intersects				
the lines.				
See sample problem #4				
5. Understand and apply				
the angle-angle				
criterion to determine				
whether two triangles				
are similar.				
See sample problem #5				

10.1f Sample Problems: Section 10.1

Sample Problem #1

Determine the measures of angles 1, 2, and 3. Justify your answers.

Sample Problem #2 In the figure to the right find the value for *x*, *y*, and *z*. Justify your answers.

ers. 133° 1 133° 2 135° 2

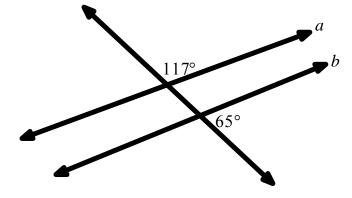
Sample Problem #3

Use the figure to the right to answer each question given that line g is parallel to line h

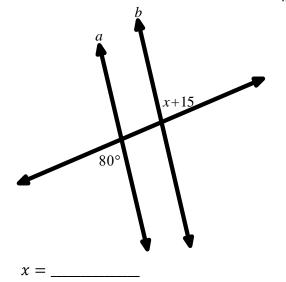
a. State the relationship between the following pairs of angles. $\angle 1$ and $\angle 8$

x = _____ *y* = _____

a. Determine if line $a \parallel$ line b. Justify your answer.

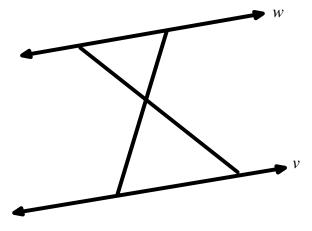


b. Find the value of x that will make line $a \parallel$ line b.



Sample Problem #5

Given that line $w \parallel$ line v, determine if the triangles formed below are similar. If they are similar justify why.



Section 10.2 The Pythagorean Theorem

Section Overview:

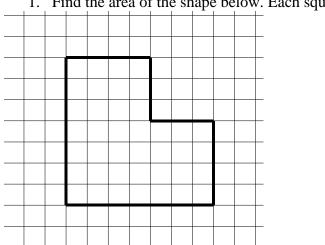
In this section students begin to formalize many of the ideas learned in Chapter 7. They will transition from using the area of a square to find the length of a segment to generalizing the relationship between the side lengths of a right triangle, i.e. the Pythagorean Theorem, to find the length of a segment. They begin this transition by finding the areas of the squares adjacent to a given right triangle. Using these concrete examples, students describe the relationship between the sides of a right triangle. From here, students work to explain a proof by picture and subsequently a paragraph proof of the Pythagorean Theorem, starting first with a right triangle of side lengths 3, 4, and 5. Students then use a similar process to explain a proof of the Pythagorean Theorem for any right triangle with side lengths a, b, and c where a and b are the legs of the right triangle and c is the hypotenuse. Students arrive at the Pythagorean Theorem: $a^2 + b^2 = c^2$ where a and b are the legs of the right triangle and c is the hypotenuse. Throughout the section, students are connecting the Pythagorean Theorem to work done in Chapter 7. Next, students use the Pythagorean Theorem to solve for the missing side length of a right triangle given the measurements of the other two sides, relying on skills learned in Chapters 7 and 8. This is followed by explaining a proof of the converse of the Pythagorean Theorem: For a triangle with side lengths a, b, and c if $a^2 + b^2 = c^2$, then the triangle is a right triangle. Using this theorem, students determine whether three given side lengths form a right triangle. Throughout this section emphasis is placed on creating good arguments and explanation. Students are not formally proving the Pythagorean Theorem and its converse but explaining why the theorems are true by learning how to provide sufficient explanations and arguments. In addition students are providing evidence and warrants for claims that they make. At the end of the section is an optional exploration on Pythagorean triples.

Concepts and Skills to Master:

By the end of this section, students should be able to:

- 1. Know that in a right triangle $a^2 + b^2 = c^2$, where *a* and *b* are the legs of the right triangle and *c* is the hypotenuse.
- 2. Understand and explain a proof of the Pythagorean Theorem.
- 3. Use the Pythagorean Theorem to solve for the missing side length of a right triangle given the measurements of the other two sides.
- 4. Understand and explain a proof of the converse of the Pythagorean Theorem. That is, for a triangle with side lengths *a*, *b*, and *c* if $a^2 + b^2 = c^2$, then the triangle is a right triangle.
- 5. Use the converse of the Pythagorean Theorem to determine whether three given measurements are possible side lengths of a right triangle.

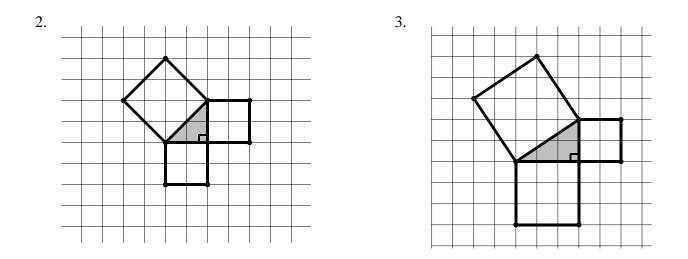
10.2a Class Activity: A Proof of the Pythagorean Theorem



1. Find the area of the shape below. Each square on the grid has a side length of 1 unit.

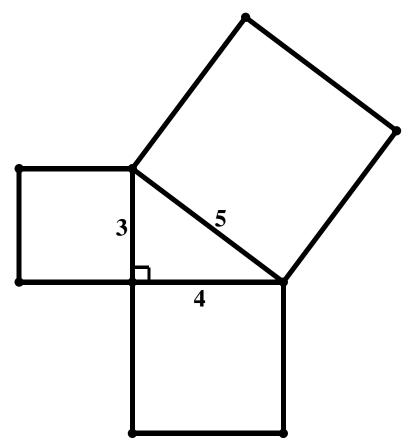
In numbers 2 and 3, a right triangle is shown in gray. The shorter sides of a right triangle are referred to as **legs**. The longer side of the right triangle (the side opposite of the right angle) is called the **hypotenuse**.

Directions: Squares have been drawn adjacent to the sides of the right triangle. Find the area of each of the squares. Assuming each square on the grid has a side length of 1 unit. Write the areas inside each of the squares.

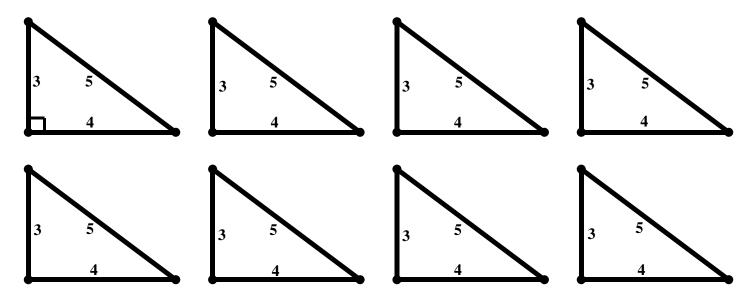


4. What do you notice about the relationship between the areas of the squares formed adjacent to the legs of a right triangle?

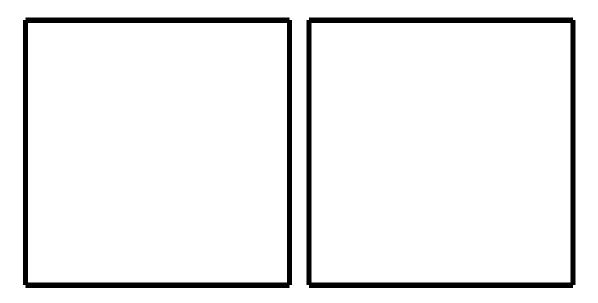
5. Below is a right triangle with side lengths 3, 4, and 5. Squares have been drawn adjacent to the sides of the right triangle.



- a. Find the area of each of the squares. Write the area inside each of the squares. Then, cut out the three squares very carefully.
- b. Below are 8 copies of the original right triangle. Cut out the 8 triangles very carefully.



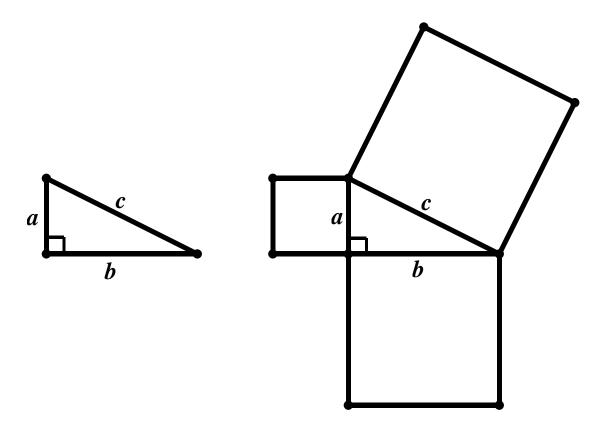
c. Below are two **congruent squares**. Since the squares are congruent, we know that their sides have the same length and subsequently they have the same area. Use your square with an area of 25 and four of the triangles from the previous page to cover one of the squares. Use your squares with areas 9 and 16 and four of the triangles from the previous page to cover the other square. Tape the pieces into place.



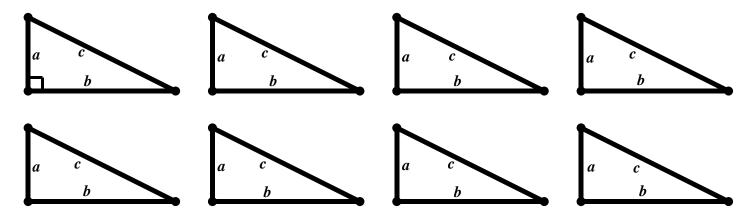
d. Use the large squares in part c) to explain the relationship you discovered in #2 – 4 between the squares formed adjacent to the sides of a right triangle.

6. In the previous problems, we saw that for specific triangles **the sum of the areas of the squares along the legs of the right triangle equals the area of the square along the hypotenuse of the triangle** by looking at several examples. Now, we want to show that this relationship holds true for *any* right triangle.

Suppose you have a right triangle with any side lengths a, b, and c where a and b are the legs of the triangle and c is the hypotenuse of the right triangle as shown below. The squares have been drawn along the sides of the right triangle. Our goal is to show that $a^2 + b^2 = c^2$ is always true.

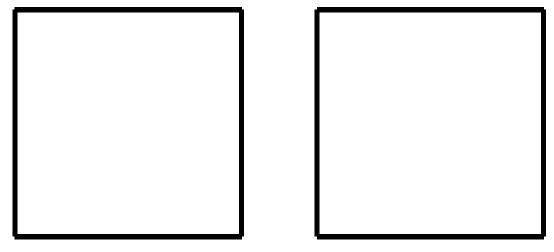


- a. Find the area of each of the squares adjacent to the sides of the right triangle. Write the areas inside each square.
- b. Cut out the squares formed on the sides of the triangle above as well as the 8 copies of the triangle with side lengths *a*, *b*, and *c* below.



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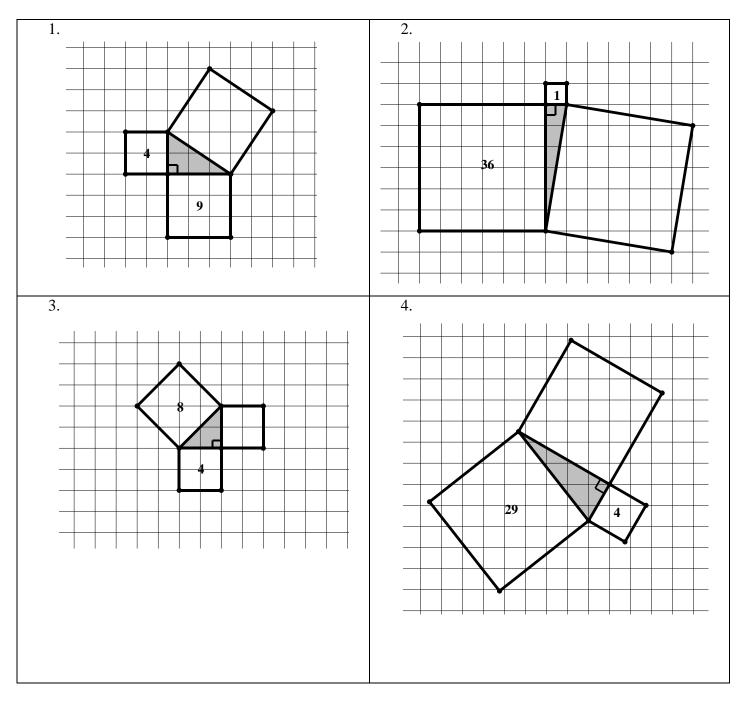
c. Arrange the 3 squares and 8 triangles to cover the 2 squares shown below.



d. Using the picture above, show that **the sum of the areas of the squares adjacent to the legs of the right triangle equals the area of the square adjacent to the hypotenuse of the triangle for <u>any</u> right triangle.**

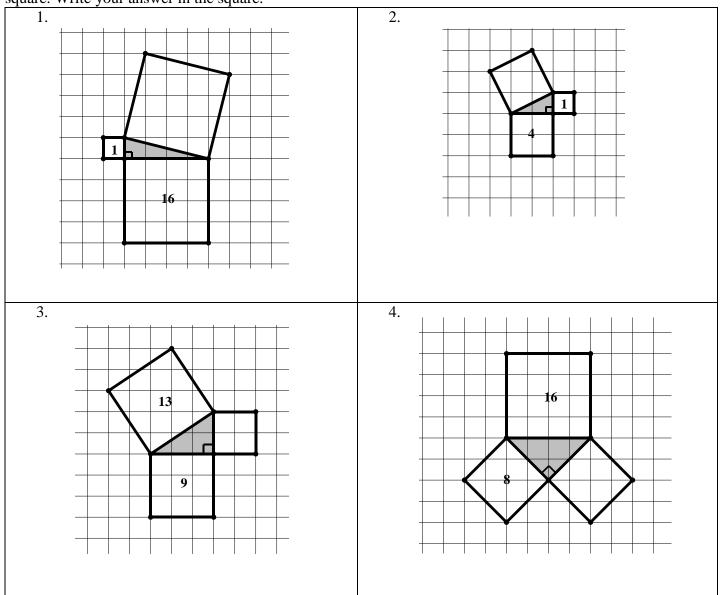
- e. Conventionally, the leg lengths of a right triangle are denoted using the variables a and b and the hypotenuse of a right triangle is denoted using the variable c. State the relationship between the side lengths of a right triangle using the words **legs** and **hypotenuse**.
- f. Write an <u>equation</u> that shows the relationship between the side lengths of a right triangle using a and b for the lengths of the legs and c for the length of the hypotenuse.

Directions: In each of the problems below, a right triangle is shown in gray. The squares along each of the three sides of the triangles have been drawn. The area of two of the squares is given. Determine the area of the third square. Write your answer in the square. Also find the side length of each square, write the sides lengths below each picture.

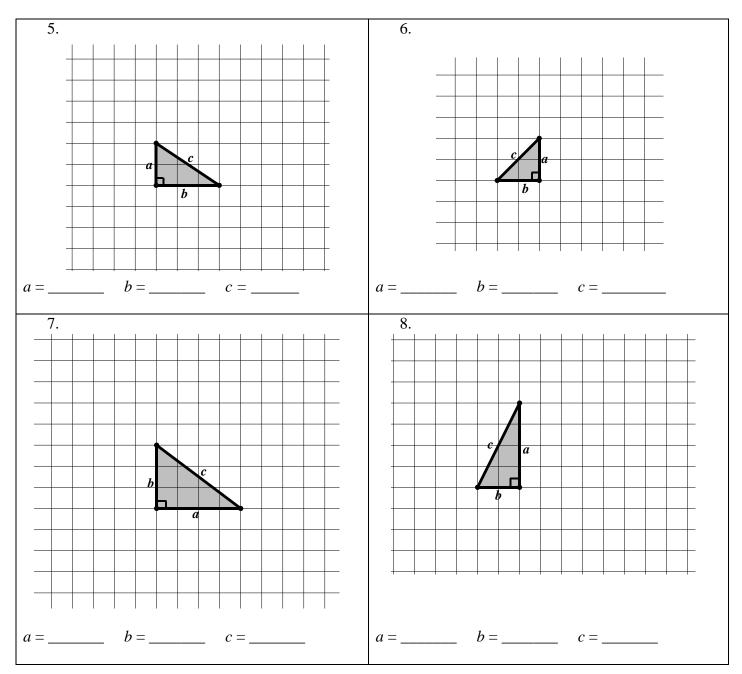


10.2a Homework: A Proof of the Pythagorean Theorem

Directions: In each of the problems below, a right triangle is shown in gray. The squares along each of the three sides of the triangles have been drawn. The area of two of the squares is given. Determine the area of the third square. Write your answer in the square.



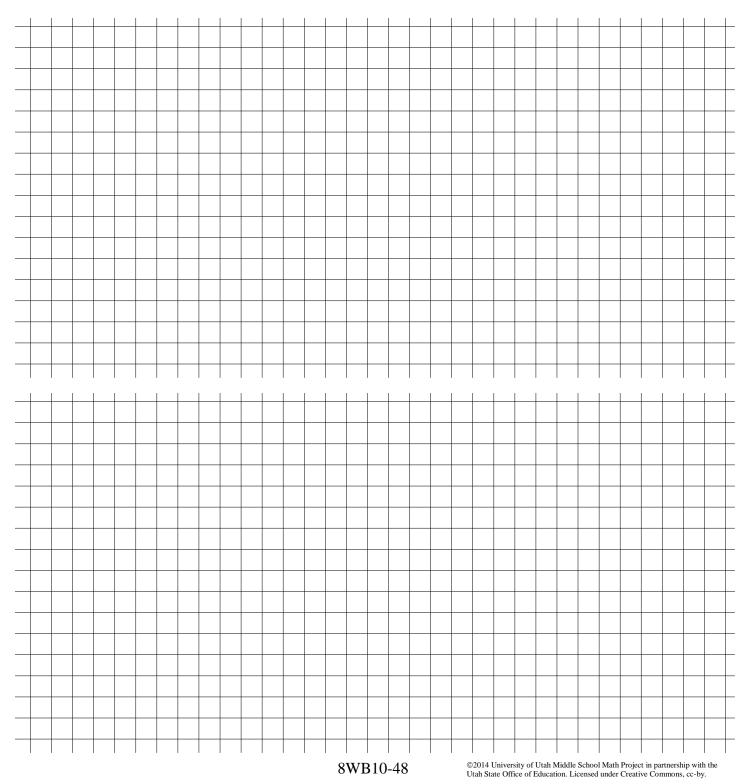
Directions: For each of the following problems, the gray triangle is a right triangle. Draw the squares adjacent to each of the three sides of the triangles. Find the area of each square and write the area in each square. Then, find the side lengths a, b, c of each triangle.



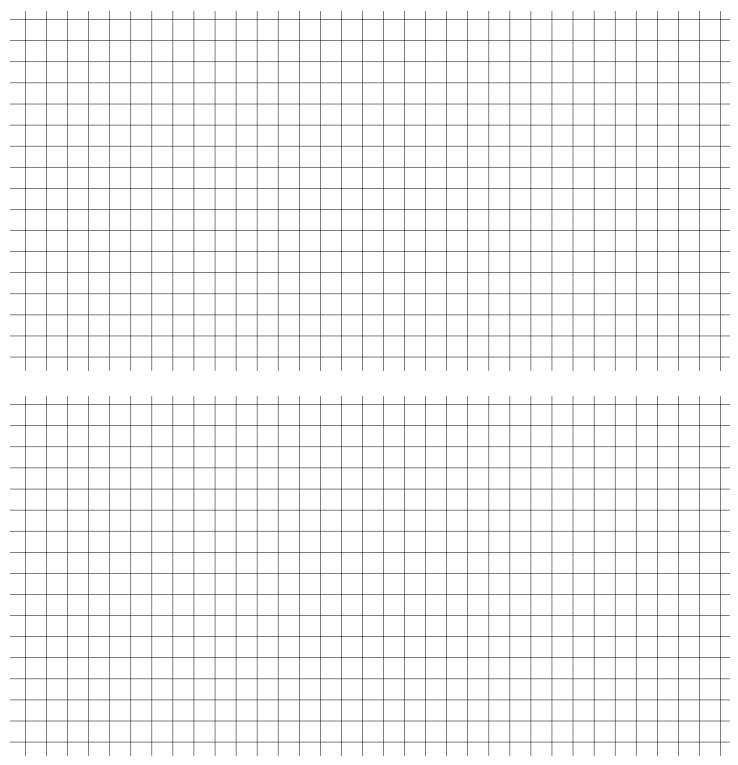
10.2b Class Activity: The Pythagorean Theorem and Tilted Squares



- 1. On the grids below, construct the following and clearly label each object:
 - a. Square ABCD that has an area of 40 square units
 - b. Square PQRS that has an area of 10 square units
 - c. \overline{EF} that has a length of $\sqrt{8}$ units
 - d. \overline{LM} that has a length of $\sqrt{17}$ units

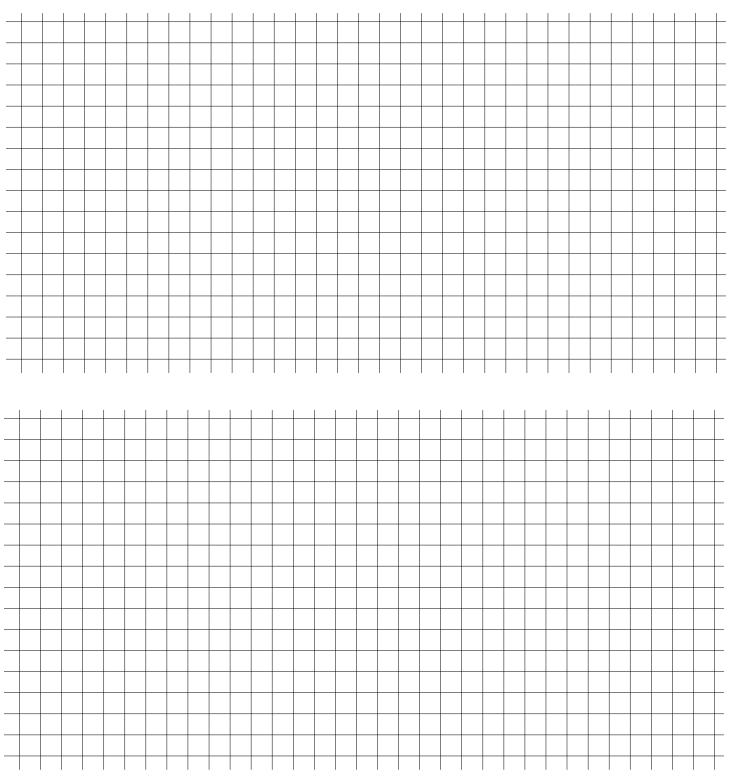


2. Draw as many different squares as you can with an area of 25 square units on the grids below. In this problem, different means that the squares are not tilted the same way.



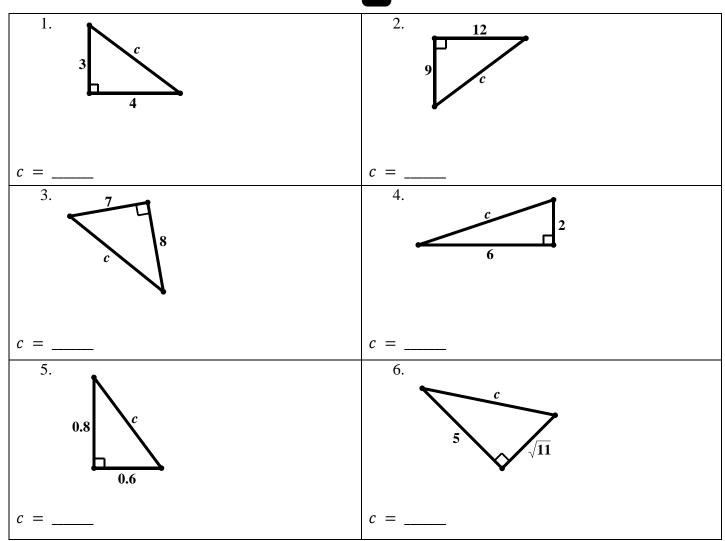
10.2b Homework: The Pythagorean Theorem and Tilted Squares

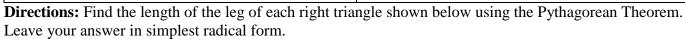
- 1. On the grids below, construct the following and clearly label each object:
 - a. Square *ABCD* that has an area of 5 square units
 - b. Square PQRS that has an area of 29 square units
 - c. \overline{EF} that has a length of $\sqrt{18}$ units
 - d. \overline{LM} that has a length of $\sqrt{13}$ units

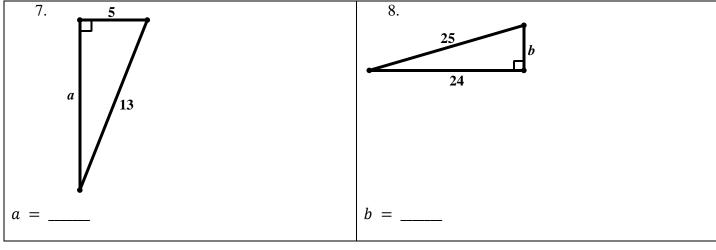


10.2c Class Activity: The Pythagorean Theorem and Unknown Side Lengths

Directions: Find the length of the hypotenuse of each right triangle shown below using the Pythagorean Theorem. Leave your answer in simplest radical form.

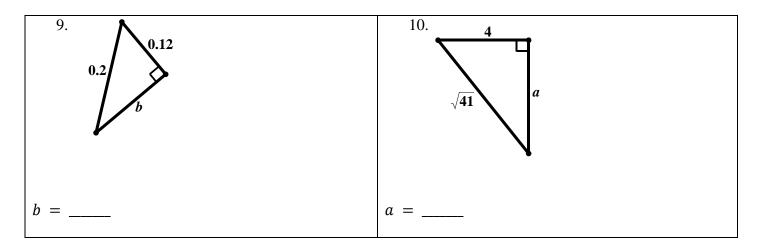




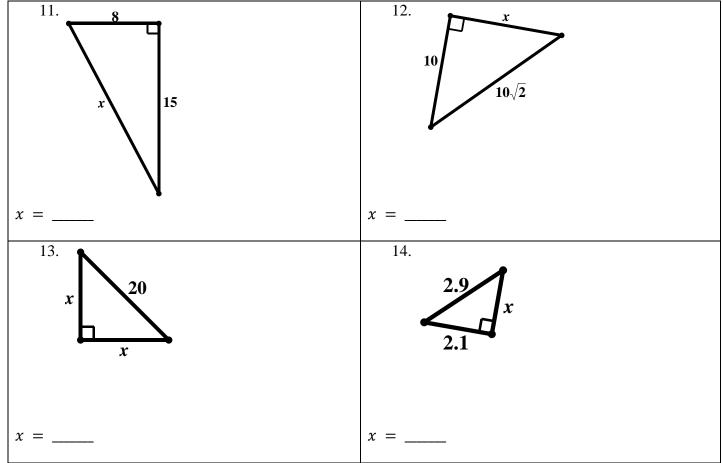


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Directions: Find the value of *x* using the Pythagorean Theorem. Leave your answer in simplest radical form.



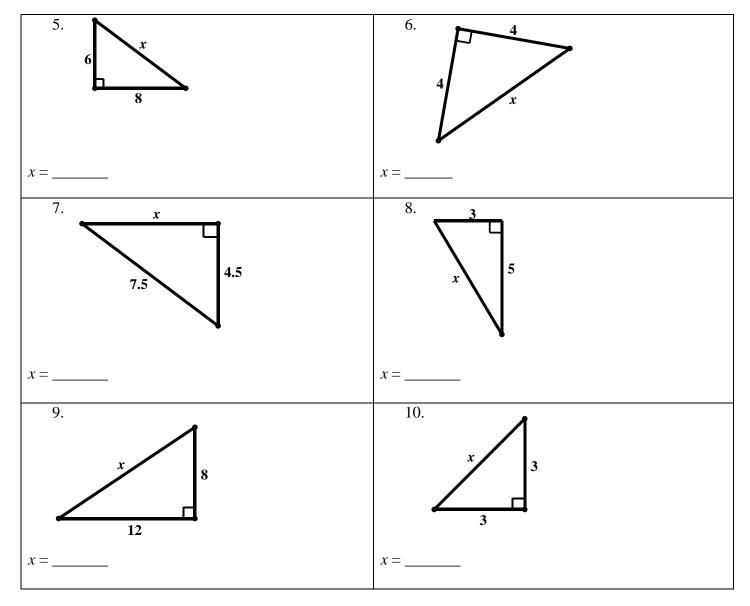
10.2c Homework: The Pythagorean Theorem and Unknown Side Lengths

Directions: Two side lengths of a right triangle have been given. Solve for the missing side length if *a* and *b* are leg lengths and *c* is the length of the hypotenuse. Leave your answer in simplest radical form.

1.
$$a = 16, b = 30, c = ?$$
 3. $a = 40, b = ?, c = 50$

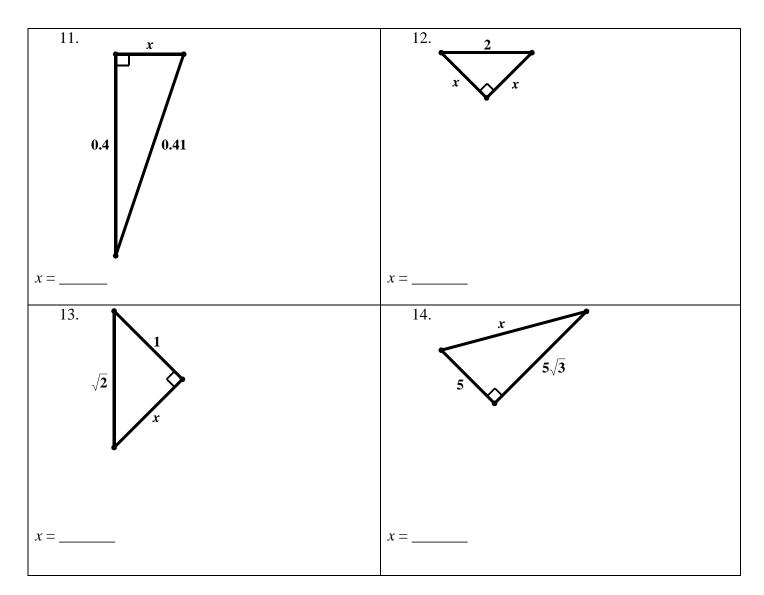
 2. $a = 2, b = 2, c = ?$
 4. $a = ?, b = 4\sqrt{3}, c = 8$

Directions: Find the value of *x* using the Pythagorean Theorem. Leave your answer in simplest radical form.

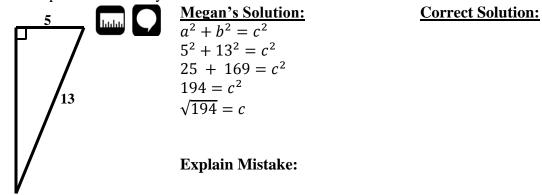


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15. **Find, Fix, and Justify:** Megan was asked to solve for the unknown side length in the triangle below. Her work is shown below. She made a mistake when solving. Explain the mistake she made and then solve the problem correctly.



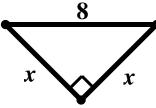
16. **Find, Fix, and Justify:** Raphael was asked to solve for the length of the hypotenuse in a right traingle with legs that have side lengths of 4 and 5. His work is shown below. He made a mistake when solving. Explain the mistake and then solve the problem correctly.

Correct Solution:

Raphael's Solution: $a^{2} + b^{2} = c^{2}$ $4^{2} + 5^{2} = c^{2}$ $16 + 25 = c^{2}$ 41 = c

Explain Mistake:

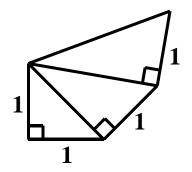
17. **Find, Fix, and Justify:** Nataani was asked to solve for the unknown side length in the triangle below. His work is shown below. He made a mistake when solving. Explain the mistake and then solve the problem correctly.



Nataani's Solution: $a^{2} + b^{2} = c^{2}$ $x^{2} + x^{2} = 8$ $2x^{2} = 8$ $x^{2} = 4$ x = 2 **Correct Solution:**

Explain Mistake:

Extra for Experts: Use the picture below to answer questions a) and b).



- a. Find all the missing side lengths and label the picture with the answers.
- b. Using the picture above, devise a strategy for constructing a segment with a length of $\sqrt{5}$. Explain your strategy below.

10.2d Class Activity: The Converse of the Pythagorean Theorem

1. Mr. Riley's 8th grade class has been studying the Pythagorean Theorem. One day, he asked his class to

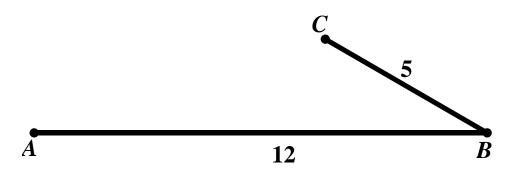
find numbers a, b, and c where $a^2 + b^2 = c^2$, and draw triangles with those side lengths.

Oscar determined that the numbers 5, 12, and 13 satisfy the Pythagorean Theorem as shown below:

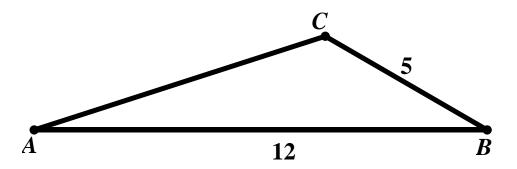
 $a^{2} + b^{2} = c^{2}$ $5^{2} + 12^{2} = 13^{2}$ 25 + 144 = 169169 = 169

Mr. Riley then said, "OK, so you have found three numbers that satisfy the Pythagorean Theorem. Now, show me that the triangle formed with these side lengths is a right triangle."

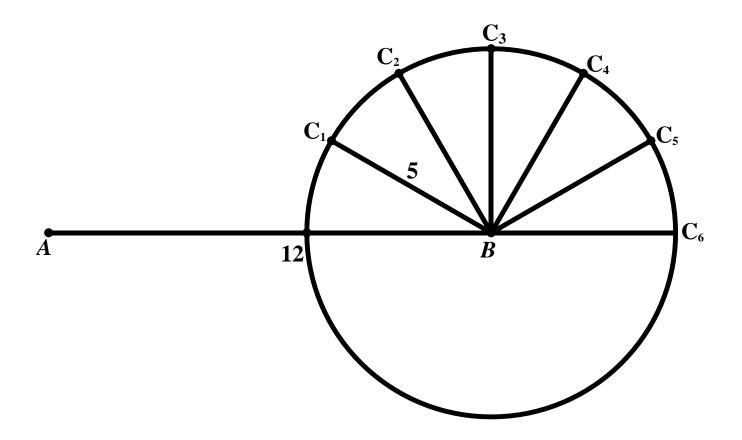
a. Oscar continued working on the problem. He constructed a segment with a length of 12 cm and labeled the segment *AB*. From the endpoint *B*, he constructed a segment with a length of 5 cm and labeled the segment *BC* as shown in the picture below. Using a ruler, verify the lengths of the segments below.



b. Then, he thought to himself, "I need to make the third side length *AC* equal to 13 because I know the triple 5, 12, 13 satisfies the Pythagorean Theorem." He connected *A* and *C* as shown below. He measured the length of *AC* and determined it did not measure 13 cm. Using a ruler, verify that *AC* does not measure 13 cm.



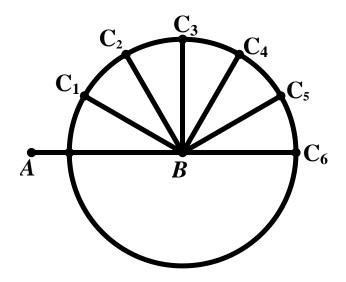
c. Then, he thought to himself, "What if I rotate \overline{BC} around point *B* until *AC* measures 13 cm?" He began to rotate \overline{BC} clockwise about *B* in increments as shown below. Help Oscar to find the location of *C* on the circle below that will give him a triangle with side lengths 5, 12, and 13.



d. What type of triangle is formed when AC equals 13 cm?

2. Lucy also found a set of numbers that satisfy the Pythagorean Theorem: 3, 4 and 5. Verify in the space below that Lucy's numbers satisfy the Pythagorean Theorem.

3. Using a process similar to Oscar's, Lucy set out to prove that a triangle with side lengths 3, 4 and 5 is in fact a right triangle. In the picture below AB = 4 cm and CB = 3 cm. Help Lucy determine the location of *C* that will create a triangle with side lengths 3 cm, 4 cm, and 5 cm.



- 4. What type of triangle is formed when AC equals 5 cm?
- 5. Based on the problems above, what type of triangle is formed with side lengths that satisfy the Pythagorean Theorem? Write down the Converse of the Pythagorean Theorem.

6. Do the side lengths given below satisfy the Pythagorean Theorem? Remember to distinguish between legs (shorter sides) and the hypotenuse (longest side) and enter them into the equation correctly.

<u>8- (8)</u>	<u> </u>
a. 11, 60, 61	b. 2, 4, 6
c. 14, 50, 48	d. 1, 3, √10;
e. 2, 4, and $2\sqrt{5}$.	f. 5, 6, 8

7. Mr. Garcia then asks the class, "What if the tick marks in Lucy's picture are each 2 cm instead of 1 cm? What are the measures of the side lengths that form the right triangle? Do they satisfy the Pythagorean Theorem?" If n# O

8. What if the tick marks in Lucy's picture are each 3 cm? 0.1 cm? 10 cm? What are the measures of the side lengths that form the right triangles given these different scales and do they satisfy the Pythagorean Theorem?

10.2d Homework: The Converse of the Pythagorean Theorem

Directions: Determine whether the three side lengths form a right triangle. Write yes or no on the line provided.

1.	9, 12, 15	2.	18, 36, 45
3.	12, 37, 35	4.	8, 15, 16
5.	$\sqrt{6}, \sqrt{10}, 4$	6.	6.4, 12, 12.2
7.	8.6, 14.7, 11.9	8.	8, 8√3, 16
9.	8, 8, 8\sqrt{2}	10	. 7, 9, 11.4

10.2e Class Activity: Exploration with Pythagorean Triples Extension

n# 🗄 🔛 🗩 💒

While we have seen several different sets of numbers that form a right triangle, there are special sets of numbers that form right triangles called Pythagorean triples. A **Pythagorean triple** is a set of nonzero **whole numbers** *a*, *b*, and *c* that can be put together to form the side lengths of a right triangle. 3, 4, 5 and 5, 12, 13 are examples of Pythagorean triples. We have seen many other sets of numbers that form a right triangle such as 0.09, 0.4, 0.41 that are not Pythagorean triples because their side lengths are not whole numbers.

a. The chart below shows some sets of numbers *a*, *b*, and *c* that are Pythagorean triples. Verify that the sets satisfy the equation $a^2 + b^2 = c^2$.

a	b	c	a ²	b ²	<i>c</i> ²
3	4	5			
5	12	13			
7	24	25			

b. Can you find additional Pythagorean triples? Explain the method you used.

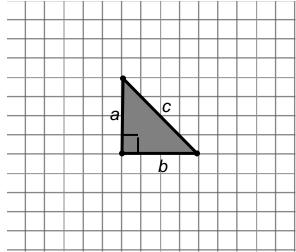
- c. The chart above starts with values for *a* that are odd numbers. Why didn't the chart start with a value of 1 for *a*.
- d. Can you find Pythagorean triples where *a* is even? What is the smallest Pythagorean triple you can find with *a* being an even number?
- e. Design a method to confirm that these numbers actually form right triangles. Write a short paragraph describing the method you used, and the results you obtained.

10.2f Self-Assessment: Section 10.2

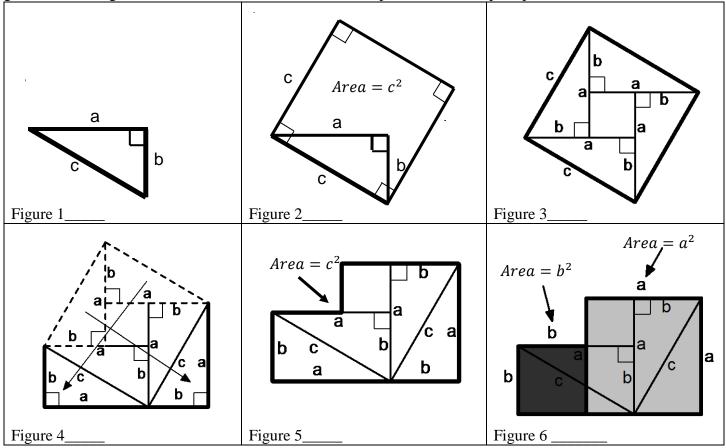
Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept. Sample problems are provided on the next page that match each skill/concept.

hat match each skill/concept.MinimalPartialSufficientSubstantial							
Skin/Concept	Understanding	Understanding	Understanding	Understanding			
	1	2	3	4			
1. Know that in a right	•	-	5	-			
triangle $a^2 + b^2 =$							
0							
c^2 , where <i>a</i> and <i>b</i> are the lass of the right							
the legs of the right							
triangle and c is the							
hypotenuse.							
See sample problem #1							
2. Understand and							
explain a proof of the							
Pythagorean							
Theorem.							
See sample problem #2							
3. Use the Pythagorean							
Theorem to solve for							
the missing side							
length of a right							
triangle given the							
measurements of the							
other two sides.							
See sample problem #3							
4. Understand and							
explain a proof of the							
converse of the							
Pythagorean							
Theorem. That is, for							
a triangle with side							
lengths a, b , and c if							
$a^2 + b^2 = c^2$, then							
the triangle is a right							
triangle.							
See sample problem #4							
5. Use the converse of							
the Pythagorean							
Theorem to determine							
whether three given							
measurements are							
possible side lengths							
of a right triangle.							
See sample problem #5							

In the picture below the gray triangle is a right triangle. Draw the squares along each of the three sides of the triangles. Find the area of each square and write the area in each square. Then, find the side lengths a, b, c of the triangle.



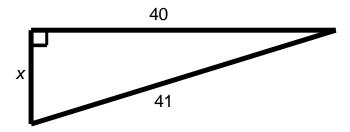
Below is a geometric explanation for a proof of the Pythagorean Theorem: Given a right triangle with side lengths *a* and *b* and a hypotenuse of *c*, then $a^2 + b^2 = c^2$. The figures for the proof are given in order. Choose the explanation that provides a sound argument accompanied with reasoning and warrants to support the claims given for each figure. Write the letter that matches each explanation in the space provided.



A. Inside of the square draw 4 congruent right triangles with side length *a* and *b* and a hypotenuse of *c*.

- B. Draw a square with off of this triangle with a side length of c. The area of square this square is c^2 . This is because the area of a square is the side length squared
- C. You can view the area of this figure as the composition of two squares with sides length *a* and *b*. The area of the darker square is b^2 and the area of the lighter shaded square is a^2 . Thus the area of the whole figure is a^2+b^2 . As stated above this is the same as the area of the original square with side length *c*. Thus $a^2 + b^2 = c^2$.
- D. Rearrange the square by translating the top two triangles to the bottom of the figure.
- E. The area of this figure is the same as the area of the original square because we have not added or removed any of the pieces.
- F. Begin with right triangle with a horizontal side length of a and a vertical side length of b and a hypotenuse of c.

Find the value of *x* using the Pythagorean Theorem. Leave your answer in simplest radical form.



The Converse of the Pythagorean Theorem states that given a triangle with side lengths *a*, *b*, and *c*, if $a^2 + b^2 = c^2$, then the triangle is a right triangle. Explain the proof of the Converse of the Pythagorean Theorem that your teacher provides for you.

Determine whether the three side lengths form a right triangle. Show your work to verify your answer.

5.5, 12.5, 13.5

Section 10.3 Applications of the Pythagorean Theorem

Section Overview:

In this section, students apply the Pythagorean Theorem to solve real-world problems in two- and threedimensions. Then, students use the Pythagorean Theorem to find the distance between two points. After the students gain an understanding of the process being used to find the distance between two points in a coordinate system, students have the opportunity to derive the distance formula from the Pythagorean Theorem and the process being used. Rather than memorizing the distance formula, the emphasis is placed on the process used to find the distance between two points in a coordinate system and the connection between the Pythagorean Theorem and the distance formula.

Concepts and Skills to Master:

By the end of this section, students should be able to:

- 1. Use the Pythagorean Theorem to solve problems in real-world contexts, including three-dimensional contexts.
- 2. Find the distance between two points in a coordinate system.

10.3a Class Activity: Applications of the Pythagorean Theorem

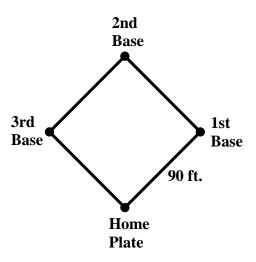
Directions: For each problem, first draw a picture if one is not provided and then solve the problem.



- 1. What is the length of the diagonal of a rectangle of side lengths 1 inch and 4 inches?
- 2. A square has a diagonal with a length of $2\sqrt{2}$ inches. What is the side length of the square?

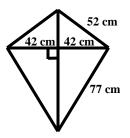
3. Two ships leave a dock. The first ship travels 6 miles east and then 8 miles north and anchors for the night. The second ship travels 5 miles west and then 12 miles south and anchors for the night. How far are each of the ships from the dock when they anchor for the night?

4. A baseball diamond is in the shape of a square. The distance between each of the consecutive bases is 90 feet. What is the distance from Home Plate to 2nd Base?



5. Ray is a contractor that needs to access his client's roof in order to assess whether the roof needs to be replaced. He sees that he can access a portion of the roof that is 15 feet from the ground. He has a ladder that is 20 feet long.

- a. How far from the base of the house should Ray place the ladder so that it just hits the top of the roof? Round your answer to the nearest tenth of a foot.
- b. How far should he place the ladder from the base of the house if he wants it to sit 3 feet higher than the top of the roof? Round your answer to the nearest tenth of a foot.
- 6. The dimensions of a kite sail are shown below. The support rod that runs from the top of the kite to the bottom of the kite has been broken and needs to be replaced. What length of rod is needed to replace the broken piece? Round your answer to the nearest tenth.

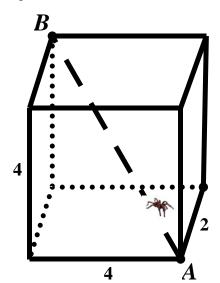


7. A new restaurant is putting in a wheelchair ramp. The landing that people enter the restaurant from is 2 feet higher than street level. Safety standards require that for every 1 foot of rise on a wheelchair ramp there must be a run of 12 feet. How long will the ramp have to be to meet safety standards? Round your answer to the nearest tenth.

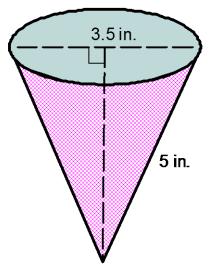
8. Melanie is having a rectangular-shaped patio built in her backyard. It is very important to Melanie that the corners of the patio are right angles. The contractor built a patio with a width of 10 feet and a length of 15 feet. The diagonal measures 20 feet. Does the patio have the right angles that Melanie requested?

9. Fred is safety conscious. He knows that to be safe, the distance between the foot of the ladder and the wall should be $\frac{1}{4}$ the height of the wall. Fred needs to get on the roof of the school building which is 20 ft. tall. How long should the ladder be if he wants it to rest on the edge of the roof and meet safety standards? Round your answer to the nearest tenth.

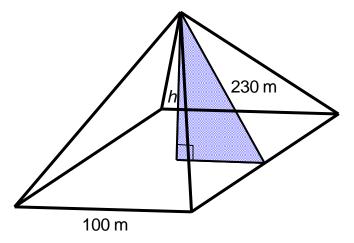
10. A spider has taken up residence in a small cardboard box which measures 2 inches by 4 inches by 4 inches. What is the length, in inches, of a straight spider web that will carry the spider from the lower right front corner of the box to the upper left back corner of the box?



11. Sunny made a paper cone to hold candy for favors for a baby shower. After making the cones she measures the slant height of the cone and the diameter of the base of the cone. Her measurements are shown in the picture below. Find the volume of the cone.



12. In the movie Despicable Me, an inflatable model of The Great Pyramid of Giza in Egypt was created by Vector to trick people into thinking that the actual pyramid had not been stolen. When inflated, the false Great Pyramid had a square base of side length 100 m. and the height of one of the side triangles was 230 meters. This is also called the slant height of the pyramid. What is the volume of gas that was used to fully inflate the fake Pyramid? (Hint: Recall the formula for the volume of a pyramid is $\frac{1}{3}Bh$ where *B* is the area of the base and *h* is the height of the pyramid (the distance from the base to the apex).



10.3a Homework: Applications of the Pythagorean Theorem

1. What is the length of the diagonal of a square with a side length of 4 cm?

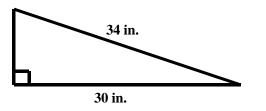
2. One side length of a rectangle is 2 inches. The diagonal of the rectangle has a length of $2\sqrt{5}$ inches. What is the length of the other side of the rectangle?

3. A football field is 360 feet long and 160 feet wide. What is the length of the diagonal of a football field assuming the field is in the shape of a rectangle?

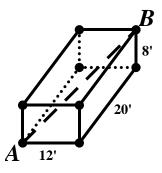
4. The length of an Olympic-size swimming pool is 55 meters. The width of the pool is 25 meters. What is the length of the diagonal of the pool assuming the pool is in the shape of a rectangle?

5. You are locked out of your house. You can see that there is a window on the second floor that is open so you plan to go and ask your neighbor for a ladder long enough to reach the window. The window is 20 feet off the ground. There is a vegetable garden on the ground below the window that extends 10 ft. from the side of the house that you can't put the ladder in. What size ladder should you ask your neighbor for?

6. Kanye just purchased a skateboarding ramp. The ramp is 34 inches long and the length of the base of the ramp is 30 inches as shown below. What is the height of the ramp?

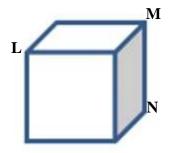


7. A rectangular-shaped room has a width of 12 feet, a length of 20 feet, and a height of 8 feet. What is the approximate distance from one corner on the floor (Point A in the figure) to the opposite corner on the ceiling (Point B in the figure)?



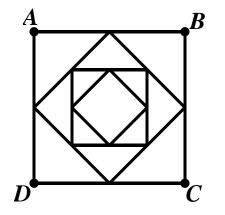
8. A large pile of sand has been dumped into a conical pile in a warehouse. The slant height of the pile is 20 feet. The diameter of the base of the sand pile is 32 ft. Find the volume of the pile of sand.

9. The cube below is a unit cube. A unit cube is a cube of side length 1.



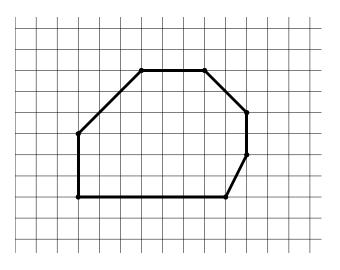
- a. What is the length of \overline{LM} ? Leave your answer in simplest radical form.
- b. What is the length of \overline{LN} ? Leave your answer in simplest radical form.

Extra for Experts: Square *ABCD* has side lengths equal to 4 inches. Connecting the midpoints of each side forms the next square inside *ABCD*. This pattern of connecting the midpoints to form a new square is repeated.



- a. What is the side length of the inner-most square?
- b. What is the area of the inner-most square?
- c. What is the ratio of the area of each square to the area of the next square created?

Extra for Experts: The following is a scale drawing of a patio that Mr. Davis plans to build in his backyard. Each box in the scale drawing represents 1 unit.



a. Find the exact value of the perimeter of the scale drawing of the patio. Show all work and thinking.

b. Find the area of the scale drawing of the patio. Show all work and thinking.

c. If the scale on the drawing above is 1 unit = 3 feet, what is the actual measure of the perimeter of the patio? The area? Show all work.

10.3b Class Activity: Finding Distance Between Two Points

B

1. Using a centimeter ruler, find the distance between the following sets of points shown below. Then draw the slope triangle of each segment, measure the lengths of the rise and run, and verify that the Pythagorean Theorem holds true.

- a. *A* to *B*
- b. *B* to *C*

A

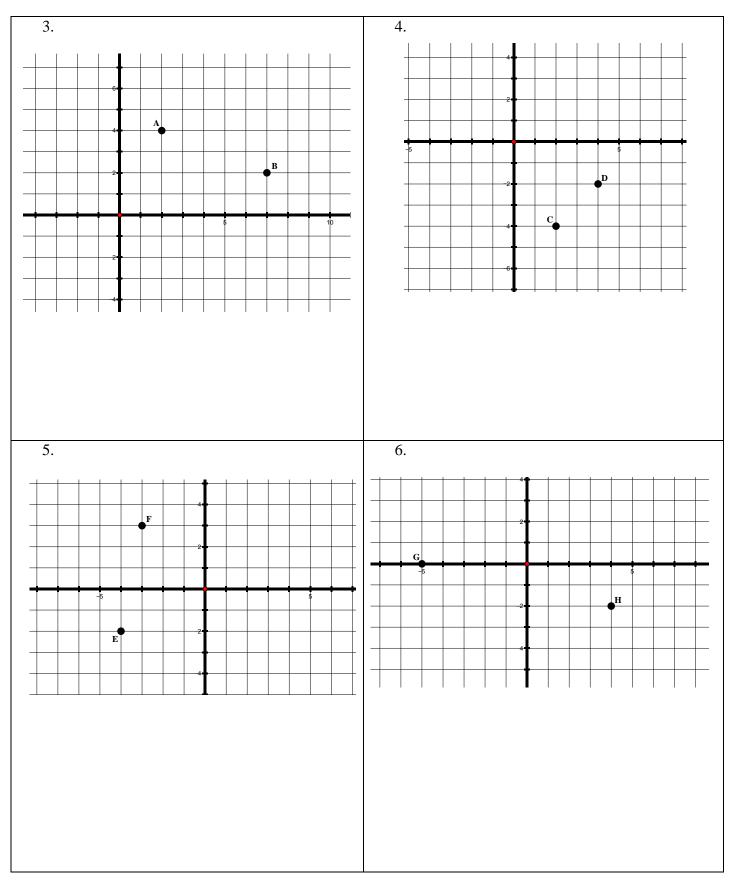
c. C to D

●D

2. Find the lengths of the segments below. Assume that each horizontal and vertical segment connecting the dots has a length of 1 unit.

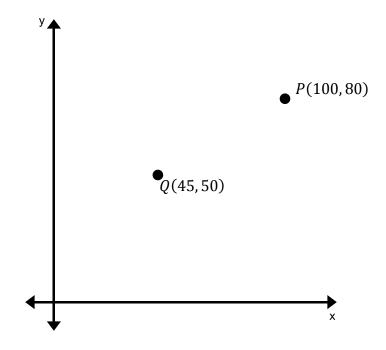
٠	•	•	•	~	•	٠	•	•	•	•	•	•	~	•	c	•	٠	•	•	•	•	٠
•	•	٠	•	•	•	b	•	•	•	•	•	•	•	•	•	-	•	•	•	•	•	•
• a		•	•	•	•	•			•	•	•	•	•	•	•	•		•	•	•	•	•
/	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•
•	•	•	•	•	•	•	•	•	•	•	•	f•	•	•	_	•	•	•	d •		•	•
•	•	•	• е	•_	_	•	•	•	-		•	•	•	•	•	•	•	•	•			•
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Directions: Label the coordinates of each point. Then, find the distance between the two points shown on each grid below.



The Coordinate Distance Formula

7. Find the distance between the two points given on the graph below.

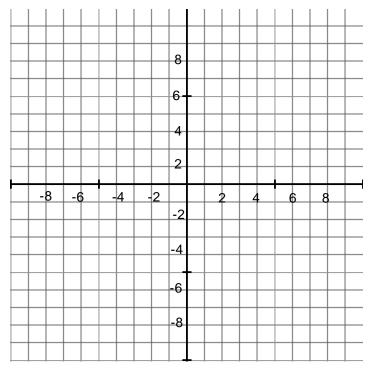


8. Find the distance between the two points given below. Leave your answers in simplest radical form.

a.
$$A:(3,5)$$
 $B:(6,9)$ b. $R:(-1,4)$ $S:(3,8)$

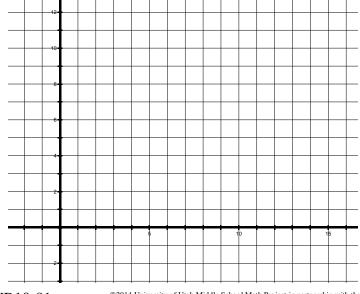
c. C: (0,5) D: (2,-3) d. S: (-3,-5) T: (2,-7)

- 9. A triangle has vertices at the points (2,3) and (4,8), and (6,3) on the coordinate plane.
 - a. Find the perimeter of the triangle. Use the grid below if needed.
 - b. Find the area of the triangle.
 - c. If the triangle is dilated by a scale factor of 3 what will the new perimeter be?
 - d. If the triangle is dilated by a scale factor of 3 what will the new area be?
 - e. Plot the original triangle, label it triangle A. Then reflect the triangle over the *y*-axis, label the new triangle A'. Does this transformation change the perimeter of the triangle? Explain your answer.



10. List **three** coordinate pairs that are 5 units away from the origin in the first quadrant. Describe how to find the points and justify your reasoning. The grid has been provided to help you.

(Note: Points on the axes are not in the first quadrant).

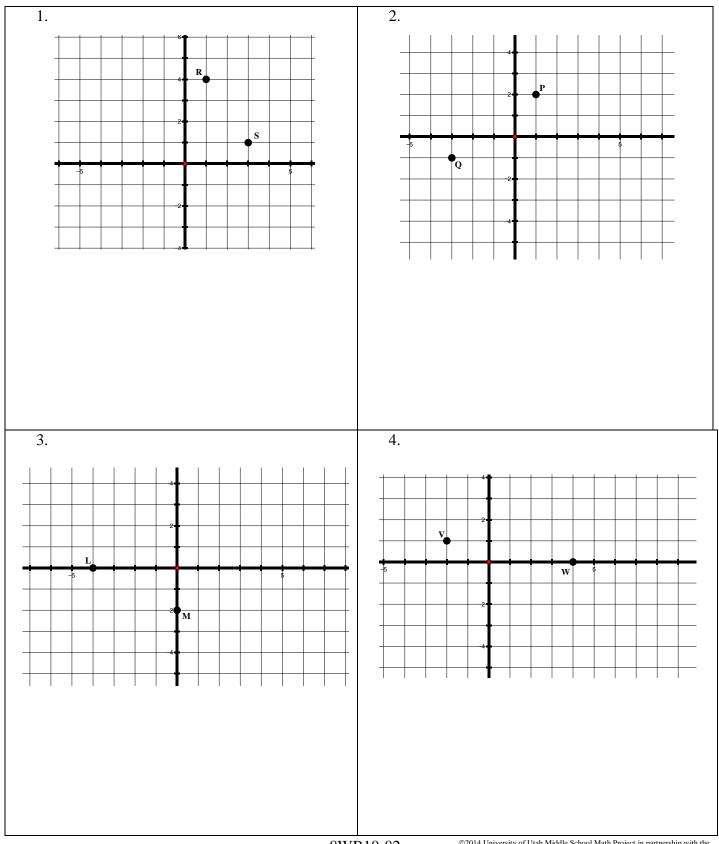


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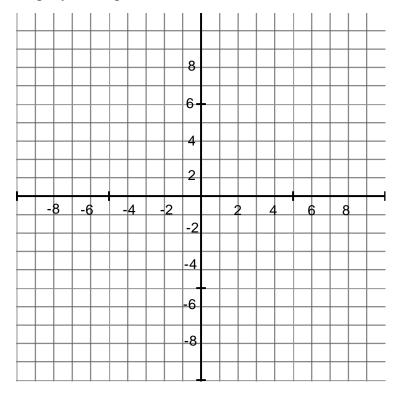
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10.3b Homework: Finding Distance Between Two Points

Directions: Find the distance between the two points shown on each grid below. Leave your answers in simplest radical form.



- 5. Find the distance between the two points given below. Leave your answers in simplest radical form.
 a. A: (2, 1) B: (4, 7)
 - b. R: (2, -1) S: (8, -7)
 - c. C:(1,0) D:(2,-3)
 - d. S: (-2, -4) T: (2, -5)
- 6. Plot any letter of the alphabet that is made up of segments that are straight lines on the coordinate plane given below. For example you can plot the letter A, E, F, etc. but not the letter B,C, D, etc.



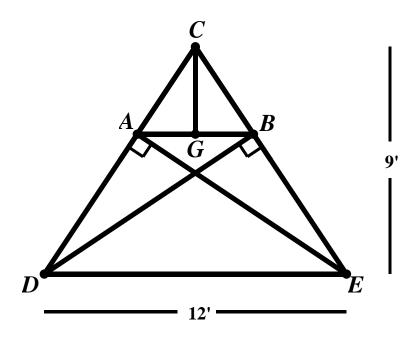
- a. Find the total distance for the segments that make up this letter.
- b. If you dilated this letter by a scale factor of 4 what is the total distance of the segments that make up your letter?
- c. If you dilated this letter by a scale factor of $\frac{1}{5}$ what is the total distance of the segments that make up your letter?
- d. Rotate your letter 180 degrees about the origin. Does this transformation change the size or shape of the letter? Explain your answer.

10.3c Extension: Construction

Mario is designing an A-frame for the lodge of a ski resort. Below is a scale drawing of his design. **Given:** *C* lies over the center of the building

$\overline{AB} \parallel \overline{DE}$

 $\angle DAE$ and $\angle EBD$ are right angles.



What are the lengths of all segments in the diagram?

10.3d Self-Assessment: Section 10.3

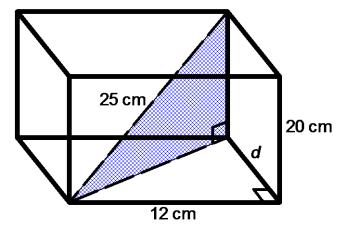
Consider the following skills/concepts. Rate your comfort level with each skill/concept by checking the box that best describes your progress in mastering each skill/concept. Sample problems are provided on the next page that match each skill/concept.

Skill/Concept	Minimal Understanding 1	Partial Understanding 2	Sufficient Understanding 3	Substantial Understanding 4
 Use the Pythagorean Theorem to solve problems in real- world contexts, including three- dimensional contexts. See sample problem #1 				
2. Find the distance between two points in a coordinate system.See sample problem #2				

10.3d Sample Problems: Section 10.3

Sample Problem #1

- a. A park is 6 miles east of your home. The bakery is 4 miles north of the park. How far is your home from the bakery as the crow flies?
- b. Find the volume of the rectangular prism given below.



Sample Problem #2

Find the distance between each set of points.

- a. A(-10,2) and B(-7,6)
- c. E(3, 5) and F(7,9)

- b. C(-2, -6) and D(6,9)
- d. G(3, 4) and H(-2, -2)

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